Update of AAPM Task Group No. 43 Report: A revised AAPM protocol for brachytherapy dose calculations

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Since publication of the American Association of Physicists in Medicine (AAPM) Task Group No. 43 Report in 1995 (TG-43), both the utilization of permanent source implantation and the number of low-energy interstitial brachytherapy source models commercially available have dramatically increased. In addition, the National Institute of Standards and Technology has introduced a new primary standard of air-kerma strength, and the brachytherapy dosimetry literature has grown substantially, documenting both improved dosimetry methodologies and dosimetric characterization of particular source models. In response to these advances, the AAPM Low-energy Interstitial Brachytherapy Dosimetry subcommittee (LIBD) herein presents an update of the TG-43 protocol for calculation of dose-rate distributions around photon-emitting brachytherapy sources. The updated protocol (TG-43U1) includes (a) a revised definition of air-kerma strength; (b) elimination of apparent activity for specification of source strength; (c) elimination of the anisotropy constant in favor of the distance-dependent one-dimensional anisotropy function; (d) guidance on extrapolating tabulated TG-43 parameters to longer and shorter distances; and (e) correction for minor inconsistencies and omissions in the original protocol and its implementation. Among the corrections are consistent guidelines for use of point- and line-source geometry functions. In addition, this report recommends a unified approach to comparing reference dose distributions derived from different investigators to develop a single critically evaluated consensus dataset as well as guidelines for performing and describing future theoretical and experimental single-source dosimetry studies. Finally, the report includes consensus datasets, in the form of dose-rate constants, radial dose functions, and one-dimensional (1D) and two-dimensional (2D) anisotropy functions, for all low-energy brachytherapy source models that met the AAPM dosimetric prerequisites as of July 15, 2001. These include the following 125I sources: Amersham Health models 6702 and 6711, Best Medical model 2301, North American Scientific Inc. (NASI) model MED3631-A/M, Bebig/Theragenics model I25.S06, and the Imagyn Medical Technologies Inc. isostar model IS-12501. The 103Pd sources included are the Theragenics Corporation model 200 and NASI model MED3633. The AAPM recommends that the revised dose-calculation protocol and revised source-specific dose-rate distributions be adopted by all end users for clinical treatment planning of low energy brachytherapy interstitial sources. Depending upon the dose-calculation protocol and parameters currently used by individual physicists, adoption of this protocol may result in changes to patient dose calculations. These changes should be carefully evaluated and
reviewed with the radiation oncologist preceding implementation of the current protocol. © 2004 American Association of Physicists in Medicine. [DOI: 10.1118/1.1646040]

Key words: TG-43, brachytherapy dosimetry protocol, TLD dosimetry, Monte Carlo calculations, $^{125}$I, $^{103}$Pd

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### I. INTRODUCTION

In 1995, the American Association of Physicists in Medicine (AAPM) Task Group No. 43 published a protocol (TG-43)\(^{1}\) introducing a new brachytherapy dose calculation formalism based largely on findings of the Interstitial Collaborative Working Group (ICWG).\(^{2}\) Previous calculation formalisms were based upon apparent activity ($A_{\text{app}}$), equivalent mass of radium, exposure-rate constants, and tissue-attenuation coefficients. These older formalisms did not account for source-to-source differences in encapsulation or internal construction. Except for radium, the exposure-rate constants and other input parameters to these algorithms depended only on the radionuclide.\(^{3}\) In contrast, TG-43 employed dose-rate constants and other dosimetric parameters that depended on the specific source design, and are directly measured or calculated for each source design. Additionally, TG-43 presented consensus dosimetry data, in terms of the recommended formalism, for the three low-energy photon emitting source models then available (Theragenics Corporation model 200 $^{103}$Pd source and Amersham Health models 6702 and 6711 $^{125}$I sources). (Certain commercial equipment, instruments, and materials are identified in this work in order to specify adequately the experimental procedure. Such identification does not imply recommendation nor endorsement by either the AAPM or National Institute of Standards and Technology (NIST), nor does it imply that the material or equipment identified is necessarily the best available for these purposes.) These data were based upon a critical review of ICWG measured dose-rate distributions using LiF TLD as well as other measurements and Monte Carlo calculations available in the literature. Overall, the TG-43 protocol has resulted in significant improvements in the standardization of both dose-calculation methodologies as well as dose-rate distributions used for clinical implementation of brachytherapy. For example, the differences between the previously used dose-rate distributions and those recommended by
TG-43 were as large as 17% for some sources. These changes have been exhaustively reviewed by the physics community and are generally accepted. Most treatment planning software vendors have implemented the TG-43 formalism and the recommended dosimetry parameters in their systems. LiF TLD dose measurements and Monte Carlo dose calculations have largely replaced the semi-empirical dose-calculation models of the past.

Since publication of the TG-43 protocol over nine years ago, significant advances have taken place in the field of permanent source implantation and brachytherapy dosimetry. To accommodate these advances, the AAPM deemed it necessary to update this protocol for the following reasons:

(a) To eliminate minor inconsistencies and omissions in the original TG-43 formalism and its implementation.4–6

(b) To incorporate subsequent AAPM recommendations, addressing requirements for acquisition of dosimetry data as well as clinical implementation.7 These recommendations, e.g., elimination of $A_{\text{app}}$ (see Appendix E) and description of minimum standards for dosimetric characterization of low-energy photon-emitting brachytherapy sources,8,9 needed to be consolidated in one convenient document.

(c) To critically reassess published brachytherapy dosimetry data for the $^{125}$I and $^{103}$Pd source models introduced both prior and subsequent to publication of the TG-43 protocol in 1995, and to recommend consensus datasets where appropriate.

(d) To develop guidelines for the determination of reference-quality dose distributions by both experimental and Monte Carlo methods, and to promote consistency in derivation of parameters used in TG-43 formalism.

Updated tables of TG-43 parameters are necessary and timely to accommodate the ~20 new low-energy interstitial brachytherapy source models that have been introduced to the market since publication of TG-43 in 1995. These commercial developments are due mostly to the rapid increase in utilization of permanent prostate brachytherapy. Some of these new brachytherapy sources were introduced into clinical practice without thorough scientific evaluation of the necessary dosimetric parameters. The AAPM addressed this issue in 1998, recommending that at least one experimental and one Monte Carlo determination of the TG-43 dosimetry parameters be published in the peer-reviewed literature before using new low-energy photon-emitting sources (those with average photon energies less than 50 keV) in routine clinical practice.9 Thus, many source models are supported by multiple dosimetry datasets based upon a variety of basic dosimetry techniques. This confronts the clinical physicist with the problem of critically evaluating and selecting an appropriate dataset for clinical use. To address this problem, this protocol presents a critical review of dosimetry data for eight $^{125}$I and $^{103}$Pd source models which satisfied the aforementioned criteria as of July 15, 2001, including the three low-energy source models included in the original TG-43 protocol. The present protocol (TG-43U1) recommends a single, consensus dataset for each source model from which the 1D and 2D dose-rate distribution can be reconstructed.

Finally, methodological guidelines are presented for physicist-investigators aiming to obtain dosimetry parameters for brachytherapy sources using calculative methods or experimental techniques.

Although many of the principles and the changes in methodology might apply, beta- or neutron-emitting sources such as $^{89}$Sr, $^{32}$P or $^{252}$Cf are not considered in this protocol. A further update of this protocol is anticipated to provide consensus, single source dose distributions and dosimetry parameters for high-energy photon-emitting (e.g. $^{192}$Ir and $^{137}$Cs) sources, and to generate consensus data for low-energy photon sources that are not included in this report, yet meet the AAPM prerequisites and are posted on the AAPM/RPC Seed Registry website10 as of December 1, 2003:

1. Amersham Health, OncoSeed model 6733 $^{125}$I,
2. Best Medical model 2335 $^{103}$Pd,
3. Draximage Inc., BrachySeed model LS-1 $^{125}$I,
4. IBt, Intersource-125 model 1251L $^{125}$I,
5. IBt, Intersource-103 model 1031L $^{103}$Pd,
6. Implant Sciences Corp. I-Plant model 3500 $^{125}$I,
7. IsoAid, Advantage model 1A1-125A $^{125}$I,
8. Mills Biopharmaceuticals Inc., ProstaSeed model SL/SH-125 $^{125}$I,
9. Nucletron Corp., selectSeed model 130.002 $^{125}$I, and
10. SourceTech Medical, $^{125}$Implant model STM1251 $^{125}$I.

As indicated in the Table of Contents, this protocol is divided into various sections. Clinical medical physicists should pay special attention to Secs. III–VI due to dosimetry formalism and clinical implementation recommendations presented herein. Section II updates the clinical rationale for accurate dosimetry. The origin of consensus datasets for eight seed models is presented in Appendix A. Dosimetry investigators will find useful the detailed recommendations presented in Secs. IV and V. The description of the NIST calibration scheme is presented in Appendix B. Manufacturers of brachytherapy treatment planning software will find new recommendations in Secs. II, IV, VI, and Appendixes C–E.

II. CLINICAL RATIONALE FOR ACCURATE DOSIMETRY

While low-energy, photon-emitting brachytherapy sources have been used to treat cancers involving a variety of anatomical sites, including eye plaque therapy for choroidal
melanoma and permanent lung implants, their most frequent indication today is for the treatment of prostate cancer. Prostate cancer is the most frequent type of cancer in men in the United States with approximately 180,000 new cases incident per year and an annual death rate of about 37,000. While approximately 60% of new cases are confined to the organ at time of diagnosis, only about 2.2% of these new cases were treated with brachytherapy in 1995. Since that time, the percentage has increased to about 30% of all eligible patients receiving implants in current practice. This increase was largely due to improvements in diagnosis and case selection facilitated by introduction of the prostate specific antigen (PSA) screening test, and to improved ultrasound-guided delivery techniques. In the United States, the pioneering work was performed by a group of investigators based in Seattle. The most widely used technique utilizes transrectal ultrasound (TRUS) guided implantation of either \(^{125}\)I or \(^{103}\)Pd brachytherapy sources using a template-guided needle delivery system to avoid open surgery required by the retropubic approach.

Several studies have shown that clinical outcomes in prostate brachytherapy, both for the retropubic approach and the TRUS-guided technique, correlate with dose coverage parameters. The extensive clinical experience of Memorial Sloan Kettering Institute (1078 patients with retropubic approach surgery from 1970–1987) was reviewed by Zelefsky and Whitmore. Multivariate-analysis revealed a \(D_{90}\) implant dose of 140 Gy to be an independent predictor of recurrence-free local control at 5, 10, and 15 years \((p = 0.001)\). \(D_{90}\) is defined as the dose delivered to 90% of the prostate volume as outlined using post-implant CT images. Similarly, a review of 110 implants at Yale University using the retropubic implant approach from 1976 to 1986 reported a correlation \((p = 0.02)\) of recurrence-free local control after 10 years with \(V_{100}\); \(V_{100}\) is defined as the percentage of target volume receiving the prescribed dose of 160 Gy.

Two recent retrospective studies of the TRUS technique demonstrate that the clinical outcome depends on dose delivered and prostate volume coverage. Stock et al. reported on an experience of 134 prostate cancer patients implanted with \(^{125}\)I and not treated with teletherapy or hormonal therapy. They assessed rates of freedom from biochemical failure as a function of the \(D_{90}\) dose. A significant increase in freedom from biochemical failure (92% vs 68% after 4 years) was observed \((p = 0.02)\) for patients \((n = 69)\) where \(D_{90} \geq 140\) Gy. Potters et al. recently reviewed the impact of various dosimetry parameters on biochemical control for their experience of 719 patients treated with permanent prostate brachytherapy. Many of these patients also received teletherapy (28%) or hormone therapy (35%). Furthermore, 84% of the implants used \(^{103}\)Pd with the remainder using \(^{125}\)I. Their results indicated that patient age, radionuclide selection, and use of teletherapy did not significantly affect biochemical relapse-free survival (PSA–RFS). The only dose-specification index that was predictive of PSA–RFS was \(D_{90}\).

Like the other two studies, studies by Stock et al. and Potters et al. were based on pre-TG-43 prescription doses of 160 Gy, and both indicated a steep dependence of clinical outcome with dose in the range of 100 to 160 Gy. For example, Stock reported freedom from biochemical failure rates of 53%, 82%, 80%, 95%, and 89% for patients receiving \(D_{90} < 100\) Gy, \(100 \leq D_{90} < 120\) Gy, \(120 \leq D_{90} < 140\) Gy, \(140 \leq D_{90} < 160\) Gy and \(D_{90} \geq 160\) Gy, respectively. The close correlation between \(D_{90}\) and PSA–RFS, and a dose response in the clinical dose range of 100 to 160 Gy are strong justifications for improved accuracy in the dosimetry for interstitial brachytherapy, which is the focus of this work. The updated dosimetry formalism and changes in calibration standards recommended herein will result in changes to the clinical practice of brachytherapy. The clinical medical physicist is advised that guidance on prescribed-to-administered dose ratios for \(^{125}\)I and \(^{103}\)Pd will be forthcoming in a subsequent report.

III. TASK GROUP # 43 DOSIMETRY FORMALISM

As in the original TG-43 protocol, both 2D (cylindrically symmetric line source) and 1D (point source) dose-calculation formalisms are given. To correct small errors and to better address implementation details neglected in the original protocol, all quantities are defined. Throughout this protocol, the following definitions are used:

1. A source is defined as any encapsulated radioactive material that may be used for brachytherapy. There are no restrictions on the size or on its symmetry.

2. A point source is a dosimetric approximation whereby radioactivity is assumed to subtend a dimensionless point with a dose distribution assumed to be spherically symmetric at a given radial distance \(r\). The influence of inverse square law, for the purpose of interpolating between tabulated transverse-plane dose-rate values, can be calculated using \(1/r^2\).

3. The transverse-plane of a cylindrically symmetric source is that plane which is perpendicular to the longitudinal axis of the source and bisects the radioactivity distribution.

4. A line source is a dosimetric approximation whereby radioactivity is assumed to be uniformly distributed along a 1D line-segment with active length \(L\). While not accurately characterizing the radioactivity distribution within an actual source, this approximation is useful in characterizing the influence of inverse square law on a source’s dose distribution for the purposes of interpolating between or extrapolating beyond tabulated TG-43 parameter values within clinical brachytherapy treatment planning systems.

5. A seed is defined as a cylindrical brachytherapy source with active length, \(L\), or effective length, \(L_{eff}\) (described later in greater detail) less than or equal to 0.5 cm.

These parameters are utilized by the TG-43U1 formalism in the following sections.
A. General 2D formalism

The general, two-dimensional (2D) dose-rate equation from the 1995 TG-43 protocol is retained,

\[ D(r, \theta) = S_K \cdot A \cdot \frac{G_L(r, \theta)}{G_L(r_0, \theta_0)} \cdot g_L(r) \cdot F(r, \theta), \]

(1)

where \( r \) denotes the distance (in centimeters) from the center of the active source to the point of interest, \( r_0 \) denotes the reference distance which is specified to be 1 cm in this protocol, and \( \theta \) denotes the polar angle specifying the point-of-interest, \( P(r, \theta) \), relative to the source longitudinal axis. The reference angle, \( \theta_0 \), defines the source transverse plane, and is specified to be 90° or \( \pi/2 \) radians (Fig. 1).

In clinical practice, source position and orientation are identified by means of radio-opaque markers. Generally, these markers are positioned symmetrically within the source capsule such that the marker, the radioactivity distribution, and the capsule have the same geometric center on the symmetry axis of the source. Thus, determination of the location of the radioisotope distribution is based upon identification of the radio-opaque markers. All sources discussed in this document can be accurately represented by a capsule and radio-opaque markers that are symmetric with respect to the transverse plane, which by definition bisects the active source and specifies the origin of the dose-calculation formalism. However, Eq. (1) can accommodate sources that are asymmetric with respect to the transverse plane. For sources that exhibit all of the following characteristics: (i) the radioactivity distribution is clearly asymmetric with respect to the planes bisecting the capsule or marker; (ii) the extent of asymmetry is known \textit{a priori} or can be measured via imaging; and (iii) the source orientation can be determined under clinical implant circumstances (e.g., via CT or radiography), then the source coordinate system origin should be positioned at the geometric center of the radionuclide distribution (as determined using positioning information obtained from the markers), not the geometric center of the exterior surface of the capsule or marker. If radio-opaque markers do not facilitate identification of source orientation and the asymmetrical distribution under clinical circumstances, then the geometric center of the source must be presumed to reside at the radio-opaque marker centroid as is conventionally performed.

The quantities used in Eq. (1) are defined and discussed later. This formalism applies to sources with cylindrically symmetric dose distributions with respect to the source longitudinal axis. In addition, the consensus datasets presented in Sec. IV B assume that dose distributions are symmetric with respect to the transverse plane, i.e., that radioactivity distributions to either side of the transverse plane are mirror images of one another. However, this formalism is readily generalized to accommodate sources that are not symmetric with respect to the transverse plane.

Equation (1) includes additional notation compared with the corresponding equation in the original TG-43 formalism, namely the subscript “\( L \)” has been added to denote the line source approximation used for the geometry function (Sec. III A 3). For evaluation of dose rates at small and large distances, the reader is referred to Appendix C.

1. Air-kerma strength

This protocol proposes minor revisions to the definition of air-kerma strength, \( S_K \), which was first introduced by the AAPM TG-32 report in 1987.\textsuperscript{22} Air-kerma strength has units of \( \mu \text{Gy m}^{-2} \text{h}^{-1} \) and is numerically identical to the quantity Reference Air Kerma Rate recommended by ICRU 38 and ICRU 60.\textsuperscript{23,24} For convenience, these unit combinations are denoted by the symbol \( U \) where 1 U = 1 \( \mu \text{Gy m}^{-2} \text{h}^{-1} \).

Air-kerma strength, \( S_K \), is the air-kerma rate, \( \dot{K}_g(d) \), \textit{in vacuo} and due to photons of energy greater than \( \delta \), at distance \( d \), multiplied by the square of this distance, \( d^2 \).

\[ S_K = \dot{K}_g(d) d^2. \]

(2)

The quantity \( d \) is the distance from the source center to the point of \( \dot{K}_g(d) \) specification (usually but not necessarily associated with the point of measurement) which should be located on the transverse plane of the source. The distance \( d \) can be any distance that is large relative to the maximum linear dimension of the radioactivity distribution so that \( S_K \) is independent of \( d \). \( \dot{K}_g(d) \) is usually inferred from transverse-plane air-kerma rate measurements performed in a free-air geometry at distances large in relation to the maximum linear dimensions of the detector and source, typically of the order of 1 meter. The qualification “\textit{in vacuo}” means that the measurements should be corrected for photon attenuation and scattering in air and any other medium interposed between the source and detector, as well as photon scattering from any nearby objects including walls, floors, and ceilings. Of course, air-kerma rate may also be calculated to subvert some of the limitations imposed on practical measurements.\textsuperscript{25} The energy cutoff, \( \delta \), is intended to exclude low-energy or contaminant photons (e.g., characteristic x-rays originating in the outer layers of steel or titanium source cladding) that increase \( \dot{K}_g(d) \) without contributing significantly to dose at distances greater than 0.1 cm in tissue. The value of \( \delta \) is typically 5 keV for low-energy photon-emitting brachytherapy sources, and is dependent on the application.
In summary, the present definition of $S_K$ differs in two important ways from the original 1987 AAPM definition. First, the original AAPM definition of $S_K$ did not allow for a low-energy cutoff. Subsequent experience using free-air chambers as primary $S_K$ standards clearly indicates that failure to exclude nonpenetrating radiations greatly increases measurement uncertainty and invalidates theoretical dosimetry models. Second, the conditions that should prevail in an experimental determination of $S_K$ are now explicitly stated.

2. Dose-rate constant

The definition of the dose-rate constant in water, $\Lambda$, is unchanged from the original TG-43 protocol; it is the ratio of dose rate at the reference position, $P(r_0, \theta_0)$, and $S_K$. $\Lambda$ has units of cGy h$^{-1}$ U$^{-1}$ which reduces to cm$^{-2}$,

$$\Lambda = \frac{D(r_0, \theta_0)}{S_K}.$$  

The dose-rate constant depends on both the radionuclide and source model, and is influenced by both the source internal design and the experimental methodology used by the primary standard to realize $S_K$. 

In 1999, a notation was introduced, $\Lambda_{nnD,PqqS}$, to identify both the dose-rate measurements or calculations used to determine $D(r_0, \theta_0)$ and the calibration standard to which this dose rate was normalized. The subscript “D” denotes reference dose rate, “nn” denotes the year in which this reference dose rate was published (either measurement or calculation), “P” denotes the provider or origin of the source strength standard (e.g., $P=\text{“N”}$ for NIST, or $P=\text{“T”}$ for the in-house calibration-standard of Theragenics Corporation), “qq” denotes the year in which this source strength standard was implemented, and the “S” subscript denotes the word standard. For example, $\Lambda_{TLD_9795}$ indicates a dose-rate constant determined from dosimetry measurements published in 1997 and normalized to an $S_K$ traceable to the 1999 NIST standard. Additional notation may also be utilized such as $\Lambda_{TLD_97NIST}$ for the dose-rate constant for the model 6702 source published in 1997 using TLDs and the 1985 NIST standard. These notations are useful for comparing results from multiple investigators, and readily highlight features such as utilization of the calibration procedure and whether or not influence of titanium $K$-shell x rays is included.

3. Geometry function

Within the context of clinical brachytherapy dose calculations, the purpose of the geometry function is to improve the accuracy with which dose rates can be estimated by interpolation from data tabulated at discrete points. Physically, the geometry function neglects scattering and attenuation, and provides an effective inverse square-law correction based upon an approximate model of the spatial distribution of radioactivity within the source. Because the geometry function is used only to interpolate between tabulated dose-rate values at defined points, highly simplistic approximations yield sufficient accuracy for treatment planning. This protocol recommends use of point- and line-source models giving rise to the following geometry functions:

$$G_p(r, \theta) = r^{-2} \quad \text{point-source approximation},$$

$$G_L(r, \theta) = \begin{cases} \frac{\beta}{Lr \sin \theta} & \text{if } \theta \neq 0^\circ \\ (r^2 - L^2/4)^{-1} & \text{if } \theta = 0^\circ \end{cases} \quad \text{line-source approximation},$$

where $\beta$ is the angle, in radians, subtended by the tips of the hypothetical line source with respect to the calculation point, $P(r, \theta)$.

In principle, either the point-source or line-source models may be consistently implemented in both the 1D and 2D versions of the TG-43 formalism. In this case, the word “consistently” means that the geometry function used for derivation of dose rates from TG-43 parameters should be identical to that used to prepare the radial dose function and 2D anisotropy function data, including use of the same active length, $L$, used in $G(r, \theta)$. Under these conditions, TG-43 dose calculations will reproduce exactly the measured or Monte Carlo-derived dose rates from which $g(r)$ and $F(r, \theta)$ tables were derived. This protocol recommends consistent use of the line-source geometry function for evaluation of 2D dose distributions, and use of either point- or line-source geometry functions for evaluations of 1D dose distributions.

Use of such simple functions is warranted since their purpose is to facilitate interpolation between tabulated data entries for duplication of the original dosimetry results.

In the case where the radioactivity is distributed over a right-cylindrical volume or annulus, this protocol recommends taking active length to be the length of this cylinder. For brachytherapy sources containing uniformly spaced multiple radioactive components, $L$ should be taken as the effective length, $L_{\text{eff}}$, given by

$$L_{\text{eff}} = \Delta S \times N,$$

where $N$ represents the number of discrete pellets contained in the source with a nominal pellet center-to-center spacing $\Delta S$. If $L_{\text{eff}}$ is greater than the physical length of the source capsule (usually $\sim 4.5$ mm), the maximum separation (distance between proximal and distal aspects of the activity distribution) should be used as the active length, $L$. This tech-
nique avoids singularities in evaluating $G(r, \theta)$ for points of interest in tissue which are located on the hypothetical line source just beyond the tip and end of the physical source.

More complex forms of the geometry function have a role in accurately estimating dose at small distances outside the tabulated data range, i.e., extrapolating $g(r)$ and $F(r, \theta)$ to small distances. Use of such expressions is permitted. However, most commercial brachytherapy treatment planning systems support only point- or line-source geometry functions. Therefore, it is the responsibility of the physicist to transform the tabulated TG-43 parameters given in this protocol, which are based upon point- and line-source approximations, to a format consistent with more complex geometry functions that may be available on their treatment planning systems.

4. Radial dose function

The radial dose function, $g_X(r)$, accounts for dose fall-off on the transverse-plane due to photon scattering and attenuation, i.e., excluding fall-off included by the geometry function. $g_X(r)$ is defined by Eq. (6), and is equal to unity at $r_0 = 1$ cm.

$$g_X(r) = \frac{\hat{D}(r, \theta_0) - G_X(r, \theta_0)}{\hat{D}(r_0, \theta_0) - G_X(r_0, \theta_0)}.$$  \hspace{1cm} (6)

The revised dose-calculation formalism has added the subscript “X” to the radial dose function and geometry function to indicate whether a point-source, “P,” or line-source, “L,” geometry function was used in transforming the data. Consequently, this protocol presents tables of both $g_P(r)$ and $g_L(r)$ values.

Equation (7) corrects a typographical error in the original TG-43 protocol. While table lookup via linear interpolation or any appropriate mathematical model fit to the data may be used to evaluate $g_X(r)$, some commercial treatment planning systems currently accommodate a fifth-order polynomial fit to the tabulated $g(r)$ data. Since this type of polynomial fit may produce erroneous results with large errors outside the radial range used to determine the fit, alternate fitting equations have been proposed which are less susceptible to this effect,

$$g_X(r) = a_0 + a_1 r + a_2 r^2 + a_3 r^3 + a_4 r^4 + a_5 r^5.$$  \hspace{1cm} (7)

Parameters $a_0$ through $a_5$ should be determined so that they fit the data within ±2%. Also, the radial range over which the fit meets this specification should be clearly specified.

5. 2D anisotropy function

The 2D anisotropy function, $F(r, \theta)$, is defined as

$$F(r, \theta) = \frac{\hat{D}(r, \theta) - G_L(r, \theta_0)}{\hat{D}(r_0, \theta_0) - G_L(r_0, \theta_0)}. $$ \hspace{1cm} (8)

Other than inclusion of the subscript $L$, this definition is identical to the original TG-43 definition. The 2D anisotropy function describes the variation in dose as a function of polar angle relative to the transverse plane. While $F(r, \theta)$ on the transverse plane is defined as unity, the value of $F(r, \theta)$ off the transverse plane typically decreases as (i) $r$ decreases, (ii) as $\theta$ approaches $0^\circ$ or $180^\circ$, (iii) as encapsulation thickness increases, and (iv) as photon energy decreases. However, $F(r, \theta)$ may exceed unity at $|\theta-90^\circ| > \pm \arcsin(L/2r)$ for right-cylinder sources coated with low-energy photon emitters due to screening of photons by the active element at angles towards the transverse plane.

As stated earlier, the active length, $L$, used to evaluate $G_L(r, \theta)$ in Eq. (4) shall be the same $L$ used to extract $g_L(r)$ and $F(r, \theta)$ from dose distributions via Eqs. (6) and (8), respectively. Otherwise, significant errors in dosimetry results at small distances may arise. For example, at $r = 0.5$ cm, a change in $L$ from 3 to 5 mm results in a 5% change in $G_L(r, \theta_0)$.

B. General 1D formalism

While a 1D isotropic point-source approximation [Eq. (9)] only approximates the true complex 2D dose distribution, it simplifies source localization procedures by eliminating the need to determine the orientation of the source longitudinal axis from imaging studies.

$$\hat{D}(r) = S_K \cdot \Lambda \cdot \frac{G_X(r, \theta_0)}{G_X(r_0, \theta_0)} \cdot g_X(r) \cdot \phi_m(r).$$ \hspace{1cm} (9)

Users should adopt one of the following implementations of Eq. (9):

$$\hat{D}(r) = S_K \cdot \Lambda \cdot \left[ \frac{r_0}{r} \right]^2 \cdot g_P(r) \cdot \phi_m(r),$$ \hspace{1cm} (10)

or

$$\hat{D}(r) = S_K \cdot \Lambda \cdot \frac{G_L(r, \theta_0)}{G_L(r_0, \theta_0)} \cdot g_L(r) \cdot \phi_m(r).$$ \hspace{1cm} (11)

While most treatment planning systems use the implementations in Eq. (10), we recommend use of Eq. (11) due to improved accuracy at small distances, e.g., $r < 1$ cm. Linear interpolation may be used to match the grid spacing of $g_X(r)$ with the grid spacing of $\phi_m(r)$.

These revised formulations require consistency between the geometry function used for dose calculation and the geometry function used for extracting $g_X(r)$ from the transverse-plane dose distribution. Furthermore, these revised formulations correct an inconsistency in Eq. (11) of the original TG-43 protocol that indirectly recommended the following incorrect equation:

$$\hat{D}(r) = S_K \cdot \Lambda \cdot \frac{G_P(r, \theta_0)}{G_P(r_0, \theta_0)} \cdot g_L(r) \cdot \phi_m(r)$$ \hspace{1cm} (not recommended). \hspace{1cm} (12)

While use of the wrong $g_X(r)$ datasets will typically give errors in the calculated dose rate of less than 2% at distances beyond 1 cm, average errors of 3%, 15%, and 74% arise at distances of 0.5, 0.25, and 0.1 cm, respectively. Clinical uti-
lization of the 1D dosimetry formalism presented in Eq. (12), or other formalisms that inconsistently apply the geometry function, are not recommended.

1. 1D anisotropy function

The 1D anisotropy function, \( \phi_{an}(r) \), is identical to the anisotropy factor defined by the original TG-43 protocol. At a given radial distance, \( \phi_{an}(r) \) is the ratio of the solid-angle-weighted dose rate, averaged over the entire \( 4 \pi \) steradian space, to the dose rate at the same distance \( r \) on the transverse plane, see Eq. (13),

\[
\phi_{an}(r) = \frac{\int_0^{2\pi} D(r, \theta) \sin(\theta) d\theta}{2D(r, \theta_0)}. \tag{13}
\]

Note that one should integrate dose rate, not the values of the 2D anisotropy function to arrive at \( \phi_{an}(r) \).

With consistent use of the geometry function, both Eqs. (10) and (11) will exactly reproduce the solid-angle weighted dose rate at a given \( r \). Of the two, Eq. (11) is recommended because the line-source geometry function will provide more accurate interpolation and extrapolation at small distances. The accuracy achievable using the 1D formalism for prostate implants was reported by Lindsay et al.\(^{33}\) and Corbett et al.\(^{34}\).

For brachytherapy treatment planning systems that do not permit entry of \( \phi_{an}(r) \), Eqs. (10) or (11) can still be implemented by carefully modifying \( g_X(r) \) to include \( \phi_{an}(r) \) as shown in Eq. (14). These modified dosimetry parameters, \( g'(r) \) and \( \phi_{an}' \), are defined as

\[
g'(r) = g_X(r) \cdot \phi_{an}(r),
\]

\[
\phi_{an}' = 1. \tag{14}
\]

While TG-43 introduced the anisotropy constant, \( \phi_{an} \), LIBD no longer recommends its use. This is discussed in greater detail in Appendix D.

IV. CONSENSUS DATASETS FOR CLINICAL IMPLEMENTATION

The \(^{125}\)I and \(^{103}\)Pd source models reviewed in this protocol (Fig. 2) satisfied the AAPM recommendations that comprehensive (2D) reference-quality dose-rate distribution data be accepted for publication by a peer-reviewed scientific journal on or before July 15, 2001. Appropriate publications can report either Monte Carlo, or experimentally derived TG-43 dosimetry parameters. As many as 12 sets of independently published data per source model were evaluated during preparation for this report. For each source model, a single consensus dataset was derived from multiple published datasets according to the following methodology.\(^{35}\) If items essential to critical evaluation were omitted, the authors were contacted for information or clarification.

(a) The peer-reviewed literature was examined to identify candidate dose distributions for each source model derived either from experimental measurements or Monte Carlo simulations. Experimentally determined values for the dose-rate constant \( (\text{EXP} \lambda) \) were averaged. Separately, \( \lambda \) values obtained using Monte Carlo techniques \( (\text{MC} \lambda) \) were averaged. The consensus value recommended in this protocol \( (\text{CON} \lambda) \) is the equally weighted average of the separately averaged experimental and Monte Carlo \( \lambda \) values. In cases where there is only one experimental result and one Monte Carlo result: \( \text{CON} \lambda = (\text{EXP} \lambda + \text{MC} \lambda)/2 \).

(b) Each candidate dataset was examined separately and eliminated from consideration if it was determined to have a problem, e.g., data inconsistency. Corrections for use of a nonliquid water measurement phantom were applied if not included in the original investigators’ analysis.

(c) For the 2D anisotropy function, \( F(r, \theta) \), and the radial dose function, \( g(r) \), all candidate datasets for a given source model were transformed using identical line-source geometry functions to permit fair comparison. The radial dose function was corrected for nonliquid water measurement medium if necessary. Assuming that the different datasets agreed within experimental uncertainties, the consensus data were defined as the ideal candidate dataset having the highest resolution, covering the largest distance range, and having the highest degree of smoothness. For most source models examined in this protocol, the consensus \( F(r, \theta) \) and \( g(r) \) data, \( \text{CON} F(r, \theta) \) and \( \text{CON} g(r) \), were taken from the transformed Monte Carlo dataset.

(d) A few entries in the tabulated consensus datasets were taken from the nonideal candidate dataset(s) to cover a larger range of distances and angles. These data were italicized to indicate that they were not directly confirmed by other measurements or calculations.

(e) The 1D anisotropy function, \( \phi_{an}(r) \), was derived using numerical integration of the dose rate, as calculated from \( \text{CON} F(r, \theta) \) dataset, with respect to solid angle. Use of the anisotropy constant, \( \phi_{an} \), is discouraged as discussed in Appendix D.

(f) When scientifically justified for a given source model, exceptions or modifications to these rules were made, and are described later. For example, if the datasets were too noisy, they were rejected.

(g) Following tabulation of \( g(r) \) and \( F(r, \theta) \) for all eight source models, overly dense datasets were downsampled to permit reasonable comparisons. Removal of a dataset point was deemed reasonable if linear interpolation using adjacent points resulted in a difference no larger than \( \pm 2\% \) of the dataset point in question. Similarly, because the various authors used different table grids, it was necessary to interpolate some of the data into the common mesh selected for presenting all eight datasets. Linear-linear interpolation was used for \( F(r, \theta) \) datasets, and log-linear interpolation was used for \( g(r) \) datasets. Interpolated data are indicated by boldface.
The details used to evaluate dosimetry parameters for each source were the following:

1. Internal source geometry and a description of the source,
2. Review of the pertinent literature for the source,
3. Correction coefficients for 1999 anomaly in NIST air-kerma strength measurements (if applicable),
4. Solid water-to-liquid water corrections,
5. Experimental method used, TLD or diode,
6. Active length assumed for the geometry function line-source approximation,
7. Name and version of the Monte Carlo transport code,
8. Cross-section library used by Monte Carlo simulation,
9. Monte Carlo estimator used to score kerma or dose, and
10. Agreement between Monte Carlo calculations and experimental measurement.

A. Source geometry variations

Source geometry and internal construction are highly manufacturer specific. Source models vary from one another with regard to weld thickness and type, radioactivity carrier construction, presence of radio-opaque material with sharp or rounded edges, the presence of silver (which produces characteristic x rays that modify the photon spectrum), and capsule wall thickness. All of these properties can affect the dosimetric characteristics of the source. Radioactive carriers may consist of a radio-transparent matrix, a radio-opaque object coated with radioactivity, or a radio-transparent matrix with highly attenuating radioactive coating. For example, the Amersham model 6702 and NASI model MED3631-A/M sources utilize spherical resin carriers coated or impregnated with radioactivity. The number of spheres varies from 3 or more...
per source. Other sources, such as the Amersham model 6711, utilize a silver rod carrier. The amount of silver, or the length of silver rod, varies by the source model. Graphite pellets are also used. For example, in the Theragenics Corporation model 200 $^{103}$Pd source, the pellets are coated with a mixture of radioactive and nonradioactive palladium.

All $^{125}$I and $^{103}$Pd source models, except for the now-obsolete model 6702 source, contain some type of radio-opaque marker to facilitate radiographic localization. For example, the graphite pellets of the Theragenics Corporation source are separated by a cylindrical lead marker. Beside the obvious dependence of photon spectrum on the radioisotope used, the backing material (e.g., the radio-opaque marker) may further perturb the spectrum. For the sources containing $^{125}$I deposited on silver, the resultant silver x rays significantly modify the effective photon spectrum. These source construction features influence the resultant dose rate distribution and the TG-43 dosimetry parameters to varying degrees. Accurate knowledge of internal source geometry and construction details is especially important for Monte Carlo modeling. Individual sources are briefly described later. References describing each source and the TG-43 parameters are given in each section. While Sec. III presented the dosimetry formalism, its applicability to the derivation of consensus datasets is given later. A detailed description for seed models is provided in Appendix A.

B. General discussion of TG-43 dosimetry parameters

1. Air-kerma strength standards

The NIST Wide-Angle Free-Air Chamber or WAFAC-based primary standard became available in 1998, and was used to standardize the $^{125}$I sources then available (models 6702, 6711, and MED3631-A/M). For a more detailed discussion of the NIST air-kerma strength standards, including those based on the Ritz free-air chamber (1985) and WAFAC (1999), see Appendix B. The WAFAC standard shifted for unknown reasons in 1999, and was corrected in the first half of 2000. For those sources available in 1998, the 1998 and 2000 WAFAC measurements agreed within estimated measurement uncertainty. Following restoration of the WAFAC to its 1998 sensitivity in 2000, all sources initially standardized against WAFAC measurements performed in 1999, and the model 3631-A/M source, which had renormalized its stated strength against the WAFAC in 1999, had to be standardized against the corrected WAFAC measurements. To implement these corrections, five sources of each type were calibrated using the NIST WAFAC and then sent to both the accredited dosimetry calibration laboratories (ADCLs) and the manufacturer for intercomparisons with their transfer standards. The AAPM Calibration Laboratory Accreditation subcommittee, in conjunction with NIST, selected the NIST WAFAC calibration date as the reference date for each source model, converting stated source strengths to the NIST WAFAC 1999 standard as corrected in 2000. This date, as described on ADCL calibration reports as the vendor traceability date, gives the date of the WAFAC calibration measurements to which the certified calibration is traceable. All vendors discussed in this protocol have agreed to accept these same WAFAC measurements as the basis for their stated source strengths. Subsequent periodic intercomparisons between NIST, ADCL, and vendor calibrations will be compared to this original reference calibration, but will not be modified unless large deviations are noted. Table I gives the NIST standard calibration date that is presently used by the ADCLs, NIST and the manufacturer for each source model along with the corresponding correction applied to $S_{\text{CON}}$ values to account for the 1999 WAFAC anomaly. The $A$ values of Table I have been corrected to the air-kerma standard specified by the WAFAC measurement performed on the listed date specified in the table. Generally, intercomparisons have agreed within ±2% of the source strengths derived from the WAFAC measurements listed in Table I. These standardization dates are subject to revision should changes in manufacturing procedures, source geometry, or the WAFAC standard itself occur that affect the accuracy of vendor or ADCL secondary standards. Future source model-specific revisions to the calibration standard could require corresponding corrections to the recommended dose-rate constant. For this reason, regular calibration comparisons among NIST, ADCL, and vendors are required.

In summary, there were two possible situations regarding the calibration of seeds at NIST using the WAFAC-based air-kerma strength standard. First, seed calibrations performed at NIST during the 1999 calendar year needed correction due to a measurement anomaly present in 1999 only. This correction was determined by another WAFAC measurement for each seed model made at a designated date in 2000 or later. Second, WAFAC measurements made prior to 1999 and after January 1, 2000 needed no correction. Since the notation $S_{K,\text{N}}$ represents the NIST WAFAC-based air-kerma strength standard as officially introduced on January 1, 1999, this notation is used for all WAFAC measurements, regardless of the date of calibration. Thus, all measured dose-rate constant data given in this protocol have been normalized to the $S_{K,\text{N}}$ standard. Any measured dose-rate constants normalized to NIST calibrations performed in 1999 have been appropriately corrected for WAFAC measurement anomalies.

2. Dose-rate constant

Specifying the dose-rate constant as accurately as possible is essential, as it is used to transform the relative TG-43 dose distribution into absolute dose rates given the air-kerma strength of the sources deployed in the patient. As discussed in more detail in Sec. V E, Monte Carlo simulations have a freedom from detector positioning and response artifacts, smaller estimated uncertainty, and can yield artifact-free dose-rate estimates at distances shorter or longer than those accessible by TLD measurement techniques. However, the accuracy of Monte Carlo is inherently limited by the investigators’ ability to accurately delineate the source internal geometry. Few Monte Carlo studies have systematically evaluated the effects of geometric uncertainty, internal component mobility, tolerances in the fabrication of sources, and
small manufacturing changes on the uncertainty of calculated dose-rate distributions. Therefore, the use of Monte Carlo values without confirmation by experimental studies is highly undesirable. Drawbacks of TLD dosimetry include (a) limited precision of repeated readings and spatial resolution; (b) a large and somewhat uncertain relative energy response correction; (c) failure of most investigators to monitor or control the composition of the measurement medium. For these reasons, the LIBD recommends using an equally weighted average of the average measured (e.g., using TLDs) and average calculated (e.g., Monte Carlo derived) values (see Table I for each source) since the two recommended dosimetry characterization techniques have complementary strengths and limitations.

The values in Table I are the average of experimental and Monte Carlo results, e.g., $CON_A$, for each source model. Experimental results normalized to the 1985 Loftus NIST standard have been corrected to agree with the NIST WAFAC 1999 standard as corrected in 2000.158 In those cases where the authors did not correct for differences between Solid Water™ and liquid water, corrections were applied based on Williamson’s Monte Carlo calculations.37 Also, a number of the cited experimental dosimetry papers published dose-rate constants are normalized to WAFAC measurements performed in 1999. In these cases, appropriate corrections were made to the published dose-rate constant values.

### 3. Radial dose function

For each source, Monte Carlo values of $g(r)$ were graphically compared with experimental values. A comparison of the Monte Carlo and experimental $g(r)$ results were expected to show an average agreement of $\pm 10\%$. While the observed differences were typically $<5\%$ for $r \leq 5 \text{ cm}$, systematic differences as large as $10\%$ were observed due to use of outdated Monte Carlo cross-section libraries. Experimental values are difficult to measure at $r < 1 \text{ cm}$, but Monte Carlo calculation of dose-rate values are often available at smaller distances. In each case, the most complete dataset (typically Monte Carlo values) was used since values were more readily available over a larger range of distances (especially at clinically significant distances closer than 1 cm) than provided by experimental measurements. The $CON_A^8(r)$ data for all $^{125}\text{I}$ and $^{103}\text{Pd}$ sources and for line- and point-source geometry functions are presented in Tables II and III, respectively. Details used in the determination of $g(r)$ for each source model are provided in Appendix A.

### 4. 2D anisotropy function

Because Monte Carlo based datasets generally have superior smoothness, spatial and angular resolution, and distance range, all anisotropy functions recommended in this protocol are derived from Monte Carlo results which have been validated by comparison to less complete experimental datasets. A graphical comparison of datasets was performed, and the agreement between the Monte Carlo datasets and the experimental datasets was again expected to be $\pm 10\%$. For $\theta > 30^\circ$, observed differences between the datasets were typically $<5\%$ with a maximum of about 9%. For $\theta \leq 30^\circ$, differences were larger (typically $\sim 10\%$ with maximum $\sim 17\%$), and are attributed to volume averaging and the high-dose-rate gradient near the source longitudinal-axis as well as uncertainties in the source geometry assumed by Monte Carlo simulations. Tables IV–XI present the $F(r, \theta)$ and $\phi_{\text{an}}(r)$ data for the sources examined herein.

### C. Uncertainty analysis

Most of the experimental and computational investigations, especially those published prior to 1999, failed to include a rigorous uncertainty analysis. Thus, the AAPM recommends that the generic uncertainty analysis described by Table XII, based on the best estimate of uncertainty of the measured dose-rate constants used to compute the $CON_A^8$ values recommended by this report, should be included henceforth. In the future, the AAPM recommends that dosimetry investigators include rigorous uncertainty analyses, specific to their methodology employed, in their published articles. Table XII, based on the works of Gearheart et al.38 and Nath and Yue,39 assigns a total $1\sigma$ uncertainty of $8\%$–$9\%$ to TLD measurements of dose-rate constant and an uncertainty of $5\%$–$7\%$ to measurements of relative quantities.

Based on results of Monroe and Williamson,37,40 purely Monte Carlo estimates of the transverse-axis dose-rate per unit air-kerma strength typically have uncertainties of $2\%$–$3\%$ at 1 cm and $3\%$–$5\%$ at 5 cm, depending on the type and magnitude of internal seed geometric uncertainties. Since relatively little has been published on estimation of
systematic (type B) uncertainties of Monte Carlo-based dose estimation, the following sections apply the principles of uncertainty analysis, as outlined in NIST Technical Note 1297,41 to estimation of total uncertainty of Monte Carlo dose-rate constants, MC\(\lambda\), Monte Carlo radial dose functions MC\(\lambda(r)\), consensus dose-rate constants, CON\(\lambda\), and absolute transverse-axis dose as evaluated by the dosimetric parameters recommended by this report.

NIST Report 1297 recommends using the Law of Propagation of Uncertainty (LPU) to estimate the uncertainty of a quantity \(Y\), that has a functional dependence on measured or estimated quantities \(x_1, \ldots, x_N\), as follows:

\[
y = f(x_1, \ldots, x_N),
\]

\[
\sigma_Y^2 = \sum_{i=1}^{N} \left( \frac{\partial f}{\partial x_i} \right)^2 \sigma_i^2 + 2 \sum_{i=1}^{N-1} \sum_{j=i+1}^{N} \frac{\partial f}{\partial x_i} \frac{\partial f}{\partial x_j} \sigma_{x_i \cdot x_j},
\]

where \(\sigma_{x_i \cdot x_j}\) (assumed zero here) represents the covariance of the two variables. For each dosimetric quantity, \(Y(\lambda, g(r), \ldots)\), the total percent uncertainty, \(\%\sigma_Y\), is considered to be composed of three sources: type B uncertainty due to uncertainty of the underlying cross sections, \(\%\sigma_{Y|\mu}\); type B uncertainties arising from uncertainty of the seed geo-

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**Table II.** Consensus \(g(r)\) values for six \(^{125}\)I sources. Interpolated data are boldface, and italicized data are nonconsensus data obtained from candidate datasets.

<table>
<thead>
<tr>
<th>(r) [cm]</th>
<th>Amersham 6702</th>
<th>Amersham 6711</th>
<th>Best 2301</th>
<th>NASI MED3631-A/M</th>
<th>Bebig IS2506</th>
<th>Imagyn IS12501</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.10</td>
<td>1.020</td>
<td>1.055</td>
<td>1.033</td>
<td>1.010</td>
<td>1.022</td>
<td></td>
</tr>
<tr>
<td>0.15</td>
<td>1.022</td>
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<td>1.029</td>
<td>\textbf{1.018}</td>
<td>1.058</td>
<td>0.809</td>
</tr>
<tr>
<td>0.25</td>
<td>\textbf{1.024}</td>
<td>1.082</td>
<td>1.027</td>
<td>0.998</td>
<td>1.030</td>
<td>1.092</td>
</tr>
<tr>
<td>0.50</td>
<td>1.030</td>
<td>1.071</td>
<td>1.028</td>
<td>1.025</td>
<td>1.030</td>
<td>1.080</td>
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<td>\textbf{1.020}</td>
<td>\textbf{1.048}</td>
</tr>
<tr>
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<td>1.000</td>
<td>1.000</td>
<td>1.000</td>
<td>1.000</td>
<td>1.000</td>
<td>1.000</td>
</tr>
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<td>0.935</td>
<td>0.908</td>
<td>0.938</td>
<td>0.954</td>
<td>0.937</td>
<td>0.907</td>
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<tr>
<td>2.00</td>
<td>0.861</td>
<td>0.814</td>
<td>0.866</td>
<td>0.836</td>
<td>0.857</td>
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<td>3.00</td>
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<td>0.689</td>
<td>0.618</td>
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<tr>
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<td>0.553</td>
<td>0.496</td>
<td>0.555</td>
<td>0.523</td>
<td>0.538</td>
<td>0.463</td>
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<tr>
<td>5.00</td>
<td>0.425</td>
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<td>0.395</td>
<td>0.409</td>
<td>0.348</td>
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<td>6.00</td>
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<td>0.320</td>
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<td>7.00</td>
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<td>9.00</td>
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<td>0.109</td>
<td>0.142</td>
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<td>10.00</td>
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<td>0.0803</td>
<td>0.103</td>
<td>0.0957</td>
<td>0.075</td>
<td>0.0986</td>
</tr>
</tbody>
</table>

---

**Table III.** Consensus \(g(r)\) values for two \(^{103}\)Pd sources. Interpolated data are boldface, and italicized data are nonconsensus data obtained from candidate datasets.

<table>
<thead>
<tr>
<th>(r) [cm]</th>
<th>Theragenics 200</th>
<th>NASI MED3633</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.10</td>
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<tr>
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<td>\textbf{1.322}</td>
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<tr>
<td>0.40</td>
<td>1.36</td>
<td>\textbf{1.286}</td>
</tr>
<tr>
<td>0.50</td>
<td>1.30</td>
<td>\textbf{1.243}</td>
</tr>
<tr>
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<td>\textbf{1.15}</td>
<td>\textbf{1.125}</td>
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<td>1.000</td>
<td>1.000</td>
</tr>
<tr>
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<td>0.770</td>
</tr>
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<tr>
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</tr>
<tr>
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<td>0.028</td>
</tr>
<tr>
<td>10.00</td>
<td>0.00615</td>
<td>0.00624</td>
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Table IV. \( F(r, \theta) \) for Amersham model 6702.

<table>
<thead>
<tr>
<th>Polar angle ( \theta ) (degrees)</th>
<th>( r ) [cm]</th>
<th>0.5</th>
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<th>2</th>
<th>3</th>
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<th>5</th>
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<td>0.569</td>
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<td>5</td>
<td>0.413</td>
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<td>0.546</td>
<td>0.586</td>
<td>0.613</td>
<td>0.631</td>
<td></td>
</tr>
<tr>
<td>10</td>
<td>0.531</td>
<td>0.584</td>
<td>0.630</td>
<td>0.660</td>
<td>0.681</td>
<td>0.697</td>
<td></td>
</tr>
<tr>
<td>15</td>
<td>0.700</td>
<td>0.700</td>
<td>0.719</td>
<td>0.738</td>
<td>0.749</td>
<td>0.758</td>
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</tr>
<tr>
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<td>0.805</td>
<td>0.810</td>
<td>0.814</td>
<td></td>
</tr>
<tr>
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<td>0.892</td>
<td>0.888</td>
<td>0.888</td>
<td>0.891</td>
<td>0.892</td>
<td>0.892</td>
<td></td>
</tr>
<tr>
<td>40</td>
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<td>0.948</td>
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<td></td>
</tr>
<tr>
<td>50</td>
<td>0.977</td>
<td>0.973</td>
<td>0.967</td>
<td>0.967</td>
<td>0.967</td>
<td>0.967</td>
<td></td>
</tr>
<tr>
<td>60</td>
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<td>0.985</td>
<td>0.983</td>
<td>0.983</td>
<td>0.983</td>
<td>0.983</td>
<td></td>
</tr>
<tr>
<td>70</td>
<td>0.996</td>
<td>0.992</td>
<td>0.990</td>
<td>0.990</td>
<td>0.990</td>
<td>0.990</td>
<td></td>
</tr>
<tr>
<td>80</td>
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<td>0.998</td>
<td>0.998</td>
<td>0.998</td>
<td>0.998</td>
<td></td>
</tr>
</tbody>
</table>

\( \phi_{\text{mp}}(r) \) 0.986 | 0.960 | 0.952 | 0.951 | 0.954 | 0.954 |

Table V. \( F(r, \theta) \) for Amersham model 6711.

<table>
<thead>
<tr>
<th>Polar angle ( \theta ) (degrees)</th>
<th>( r ) [cm]</th>
<th>0.5</th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
<th>5</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>0.333</td>
<td>0.370</td>
<td>0.442</td>
<td>0.488</td>
<td>0.520</td>
<td>0.550</td>
<td></td>
</tr>
<tr>
<td>5</td>
<td>0.400</td>
<td>0.429</td>
<td>0.497</td>
<td>0.535</td>
<td>0.561</td>
<td>0.587</td>
<td></td>
</tr>
<tr>
<td>10</td>
<td>0.519</td>
<td>0.537</td>
<td>0.580</td>
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<td>0.630</td>
<td>0.645</td>
<td></td>
</tr>
<tr>
<td>20</td>
<td>0.716</td>
<td>0.705</td>
<td>0.727</td>
<td>0.743</td>
<td>0.752</td>
<td>0.760</td>
<td></td>
</tr>
<tr>
<td>30</td>
<td>0.846</td>
<td>0.834</td>
<td>0.842</td>
<td>0.846</td>
<td>0.848</td>
<td>0.852</td>
<td></td>
</tr>
<tr>
<td>40</td>
<td>0.926</td>
<td>0.925</td>
<td>0.926</td>
<td>0.926</td>
<td>0.928</td>
<td>0.928</td>
<td></td>
</tr>
<tr>
<td>50</td>
<td>0.972</td>
<td>0.972</td>
<td>0.970</td>
<td>0.969</td>
<td>0.969</td>
<td>0.969</td>
<td></td>
</tr>
<tr>
<td>60</td>
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<td>0.987</td>
<td>0.987</td>
<td>0.987</td>
<td>0.987</td>
<td></td>
</tr>
<tr>
<td>70</td>
<td>0.996</td>
<td>0.996</td>
<td>0.996</td>
<td>0.995</td>
<td>0.995</td>
<td>0.995</td>
<td></td>
</tr>
<tr>
<td>80</td>
<td>1.000</td>
<td>1.000</td>
<td>1.000</td>
<td>0.999</td>
<td>0.999</td>
<td>0.999</td>
<td></td>
</tr>
</tbody>
</table>

\( \phi_{\text{mp}}(r) \) 0.973 | 0.944 | 0.941 | 0.942 | 0.943 | 0.944 |

Table VI. \( F(r, \theta) \) for Best model 2301.

<table>
<thead>
<tr>
<th>Polar angle ( \theta ) (degrees)</th>
<th>( r ) [cm]</th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
<th>5</th>
<th>6</th>
<th>7</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>0.367</td>
<td>0.454</td>
<td>0.922</td>
<td>0.902</td>
<td>0.894</td>
<td>0.893</td>
<td>0.858</td>
<td></td>
</tr>
<tr>
<td>5</td>
<td>0.724</td>
<td>0.720</td>
<td>0.726</td>
<td>0.738</td>
<td>0.753</td>
<td>0.771</td>
<td>0.800</td>
<td></td>
</tr>
<tr>
<td>10</td>
<td>0.653</td>
<td>0.671</td>
<td>0.699</td>
<td>0.727</td>
<td>0.732</td>
<td>0.764</td>
<td>0.782</td>
<td></td>
</tr>
<tr>
<td>20</td>
<td>0.785</td>
<td>0.794</td>
<td>0.809</td>
<td>0.814</td>
<td>0.825</td>
<td>0.852</td>
<td>0.821</td>
<td></td>
</tr>
<tr>
<td>30</td>
<td>0.900</td>
<td>0.890</td>
<td>0.885</td>
<td>0.892</td>
<td>0.899</td>
<td>0.915</td>
<td>0.873</td>
<td></td>
</tr>
<tr>
<td>40</td>
<td>0.982</td>
<td>0.954</td>
<td>0.947</td>
<td>0.939</td>
<td>0.943</td>
<td>0.976</td>
<td>0.937</td>
<td></td>
</tr>
<tr>
<td>50</td>
<td>1.014</td>
<td>0.992</td>
<td>0.985</td>
<td>0.991</td>
<td>0.997</td>
<td>0.989</td>
<td>0.961</td>
<td></td>
</tr>
<tr>
<td>60</td>
<td>1.030</td>
<td>1.010</td>
<td>1.009</td>
<td>1.007</td>
<td>1.010</td>
<td>1.019</td>
<td>1.002</td>
<td></td>
</tr>
<tr>
<td>70</td>
<td>1.036</td>
<td>1.026</td>
<td>1.016</td>
<td>1.023</td>
<td>1.011</td>
<td>1.035</td>
<td>1.010</td>
<td></td>
</tr>
<tr>
<td>80</td>
<td>1.010</td>
<td>1.030</td>
<td>1.019</td>
<td>1.017</td>
<td>1.010</td>
<td>1.020</td>
<td>1.005</td>
<td></td>
</tr>
</tbody>
</table>

\( \phi_{\text{mp}}(r) \) 0.945 | 0.987 | 0.968 | 0.971 | 0.969 | 0.991 | 0.969 |
TABLE VII. $F(r, \theta)$ for NASI model MED3631-A/M.

<table>
<thead>
<tr>
<th>Polar angle $\theta$ (degrees)</th>
<th>$r$ [cm]</th>
<th>(0.25)</th>
<th>(0.5)</th>
<th>(1)</th>
<th>(2)</th>
<th>(5)</th>
<th>(10)</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td></td>
<td>1.038</td>
<td>0.690</td>
<td>0.702</td>
<td>0.667</td>
<td>0.718</td>
<td>0.771</td>
</tr>
<tr>
<td>10</td>
<td></td>
<td>0.984</td>
<td>0.700</td>
<td>0.662</td>
<td>0.676</td>
<td>0.728</td>
<td>0.758</td>
</tr>
<tr>
<td>20</td>
<td></td>
<td>0.916</td>
<td>0.761</td>
<td>0.747</td>
<td>0.764</td>
<td>0.794</td>
<td>0.815</td>
</tr>
<tr>
<td>30</td>
<td></td>
<td>0.928</td>
<td>0.854</td>
<td>0.846</td>
<td>0.852</td>
<td>0.871</td>
<td>0.878</td>
</tr>
<tr>
<td>40</td>
<td></td>
<td>0.941</td>
<td>0.909</td>
<td>0.906</td>
<td>0.909</td>
<td>0.918</td>
<td>0.914</td>
</tr>
<tr>
<td>50</td>
<td></td>
<td>0.962</td>
<td>0.949</td>
<td>0.949</td>
<td>0.950</td>
<td>0.958</td>
<td>0.954</td>
</tr>
<tr>
<td>60</td>
<td></td>
<td>0.975</td>
<td>0.975</td>
<td>0.975</td>
<td>0.975</td>
<td>0.983</td>
<td>0.972</td>
</tr>
<tr>
<td>70</td>
<td></td>
<td>0.991</td>
<td>0.989</td>
<td>0.992</td>
<td>0.990</td>
<td>0.993</td>
<td>0.989</td>
</tr>
<tr>
<td>80</td>
<td></td>
<td>0.999</td>
<td>0.999</td>
<td>1.003</td>
<td>0.996</td>
<td>0.998</td>
<td>0.999</td>
</tr>
</tbody>
</table>

$\phi_m(r)$

|          | \(1.288\) | \(1.008\) | \(0.952\) | \(0.945\) | \(0.948\) | \(0.948\) | \(0.948\) |

TABLE VIII. $F(r, \theta)$ for Bebig/Theragenics model I25.S06. Italicized data are nonconsensus data obtained from candidate datasets.

<table>
<thead>
<tr>
<th>Polar angle $\theta$ (degrees)</th>
<th>$r$ [cm]</th>
<th>(0.25)</th>
<th>(0.5)</th>
<th>(1)</th>
<th>(2)</th>
<th>(5)</th>
<th>(7)</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td></td>
<td>0.302</td>
<td>0.429</td>
<td>0.512</td>
<td>0.579</td>
<td>0.610</td>
<td>0.649</td>
</tr>
<tr>
<td>5</td>
<td></td>
<td>0.352</td>
<td>0.436</td>
<td>0.509</td>
<td>0.576</td>
<td>0.610</td>
<td>0.635</td>
</tr>
<tr>
<td>10</td>
<td></td>
<td>0.440</td>
<td>0.476</td>
<td>0.557</td>
<td>0.622</td>
<td>0.651</td>
<td>0.672</td>
</tr>
<tr>
<td>20</td>
<td></td>
<td>0.746</td>
<td>0.686</td>
<td>0.721</td>
<td>0.757</td>
<td>0.771</td>
<td>0.785</td>
</tr>
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<td>0.886</td>
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<td>0.846</td>
<td>0.857</td>
<td>0.862</td>
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<tr>
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<td>0.943</td>
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<td>0.898</td>
<td>0.907</td>
<td>0.908</td>
<td>0.913</td>
</tr>
<tr>
<td>50</td>
<td></td>
<td>0.969</td>
<td>0.946</td>
<td>0.942</td>
<td>0.947</td>
<td>0.944</td>
<td>0.947</td>
</tr>
<tr>
<td>60</td>
<td></td>
<td>0.984</td>
<td>0.974</td>
<td>0.970</td>
<td>0.974</td>
<td>0.967</td>
<td>0.966</td>
</tr>
<tr>
<td>70</td>
<td></td>
<td>0.994</td>
<td>0.989</td>
<td>0.988</td>
<td>0.990</td>
<td>0.984</td>
<td>0.985</td>
</tr>
<tr>
<td>80</td>
<td></td>
<td>0.998</td>
<td>0.998</td>
<td>0.998</td>
<td>1.000</td>
<td>0.994</td>
<td>1.000</td>
</tr>
</tbody>
</table>

$\phi_m(r)$

|          | \(1.122\) | \(0.968\) | \(0.939\) | \(0.939\) | \(0.938\) | \(0.940\) | \(0.941\) | \(0.949\) | \(0.867\) | \(0.886\) | \(0.894\) | \(0.897\) | \(0.897\) | \(0.879\) |
metric model, \( \% \sigma_{Y|\text{geo}} \); and the type A statistical uncertainty, \( \% \sigma_{Y|\text{s}} \), inherent to the Monte Carlo technique. Applying Eq. (15), one obtains

\[
\% \sigma_Y = \sqrt{\left( \% \sigma_{Y|\mu} \right)^2 + \left( \% \sigma_{Y|\text{geo}} + \% \sigma_{Y|\text{s}} \right)^2}
\]

where the relative uncertainty propagation factor is defined as

\[
\% \sigma_Y = \frac{\partial Y}{\partial x} \cdot \frac{\sigma_Y}{Y}. \tag{17}
\]

The variable \( x \) denotes either the cross-section value, \( \mu \), or geometric dimension, geo, of interest. The uncertainties estimated here are standard uncertainties, having a coverage factor of unity, approximating a 68% level of confidence.

### 1. \( \Lambda \) uncertainty

The influence of cross-section uncertainty was derived from the Monte Carlo data published by Hedtjarn \textit{et al.}\textsuperscript{32} This paper gives Monte Carlo estimates of \( \Lambda \) and \( g(r) \) calculated for two different cross-section libraries, DLC-99 (circa 1983) and DLC-146 (1995). The photoelectric cross sections of the two libraries differ by about 2\% between 1–40 keV, corresponding to a 1.1\% change in \( \mu \) for the mean photon energy emitted by \( ^{125}I \). Using these data to numerically estimate the derivative in Eq. (17), one obtains \( \% \sigma_{\Lambda} = 0.68 \). Assuming that \( \% \sigma_{\mu} = 2\% \),\textsuperscript{33} then uncertainty in \( \Lambda \) due to cross-section uncertainty, \( \% \sigma_{\Lambda|\mu} \), is 1.4\%.

### Table X. \( F(r, \theta) \) for Theragens Corp. model 200. Italicized data are nonconsensus data obtained from candidate datasets.

<table>
<thead>
<tr>
<th>Polar angle ( \theta ) (degrees)</th>
<th>( r ) (cm)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>0.25</td>
</tr>
<tr>
<td>0</td>
<td>0.619</td>
</tr>
<tr>
<td>1</td>
<td>0.617</td>
</tr>
<tr>
<td>2</td>
<td>0.618</td>
</tr>
<tr>
<td>3</td>
<td>0.620</td>
</tr>
<tr>
<td>4</td>
<td>0.617</td>
</tr>
<tr>
<td>5</td>
<td>0.579</td>
</tr>
<tr>
<td>6</td>
<td>0.284</td>
</tr>
<tr>
<td>7</td>
<td>0.191</td>
</tr>
<tr>
<td>8</td>
<td>0.289</td>
</tr>
<tr>
<td>9</td>
<td>0.496</td>
</tr>
<tr>
<td>10</td>
<td>0.555</td>
</tr>
<tr>
<td>11</td>
<td>0.775</td>
</tr>
<tr>
<td>12</td>
<td>0.917</td>
</tr>
<tr>
<td>13</td>
<td>0.945</td>
</tr>
<tr>
<td>14</td>
<td>0.976</td>
</tr>
<tr>
<td>15</td>
<td>0.981</td>
</tr>
<tr>
<td>16</td>
<td>0.947</td>
</tr>
<tr>
<td>17</td>
<td>0.992</td>
</tr>
<tr>
<td>18</td>
<td>1.007</td>
</tr>
</tbody>
</table>

\( \phi_{\mu}(r) \)

1.300 0.880 0.859 0.855 0.870 0.884 0.895 0.897 0.918

### Table XI. \( F(r, \theta) \) for NASI model MED3633.

<table>
<thead>
<tr>
<th>Polar angle ( \theta ) (degrees)</th>
<th>( r ) (cm)</th>
</tr>
</thead>
<tbody>
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<td></td>
<td>0.25</td>
</tr>
<tr>
<td>0</td>
<td>1.024</td>
</tr>
<tr>
<td>1</td>
<td>0.888</td>
</tr>
<tr>
<td>2</td>
<td>0.850</td>
</tr>
<tr>
<td>3</td>
<td>0.892</td>
</tr>
<tr>
<td>4</td>
<td>0.931</td>
</tr>
<tr>
<td>5</td>
<td>0.952</td>
</tr>
<tr>
<td>6</td>
<td>0.971</td>
</tr>
<tr>
<td>7</td>
<td>0.995</td>
</tr>
<tr>
<td>8</td>
<td>1.003</td>
</tr>
</tbody>
</table>

\( \phi_{\mu}(r) \)

1.257 0.962 0.903 0.895 0.898 0.917
Estimation of geometric uncertainty, $\% \sigma_{\Lambda|\text{geo}}$, is a complex and poorly understood undertaking. Each source design is characterized by numerous and unique geometric parameters, most of which have unknown and potentially correlated probability distributions. However, a few papers in the literature report parametric studies, in which the sensitivity of dosimetric parameters to specified sources of geometric variability is documented. For example, Williamson has shown that the distance between the two radioactive spherical pellets of the DraxImage $^{125}$I source varies from 3.50 to 3.77 mm. This leads to a source-orientation dependent variation of approximately 5% in calculated dose-rate constant. Rivard published a similar finding for the NASI model $^{125}$I source. If this phenomenon is modeled by a Type B rectangular distribution bounded by the minimum and maximum values, the standard uncertainty is given by

$$\% \sigma_{\Lambda|\text{geo}} = 100 \frac{\Lambda_{\max} - \Lambda_{\min}}{2 \Delta V^3}. \quad (18)$$

For the DraxImage source, Eq. (18) yields a $\% \sigma_{\Lambda|\text{geo}} = 1.4\%$. For the Theragenics Corporation Model 200 seed, Williamson has shown that $\Lambda$ is relatively insensitive to Pd metal layer thickness or end weld configuration. Thus 2% seems to be a reasonable and conservative estimate of $\% \sigma_{\Lambda|\text{geo}}$.

The reported statistical precision of Monte Carlo $\Lambda$ estimates ranges from 0.5% for Williamson’s recent studies to 3% for Rivard’s MED3631-A/M study. Thus for a typical Williamson study, one obtains a $\% \sigma_{\Lambda}$ of 2.5%. Using the $\% \sigma_{\Lambda|\mu}$ reported by each investigator along with the standard

$$\% \sigma_{\Lambda|\text{geo}} \text{ and } \% \sigma_{\Lambda|\mu} \text{ values, discussed above, } \% \sigma_{\Lambda} \text{ varies from 2.5% to 3.7% for the eight seeds described in this report. Thus, assuming a standard or generic } \% \sigma_{\Lambda} \text{ of 3% for all Monte Carlo studies seems reasonable.}

### 2. CON$_\Lambda$ uncertainty

This report defines the consensus dose-rate constant as

$$\text{CON}_\Lambda = \alpha \cdot \text{EXP}_\Lambda + (1 - \alpha) \cdot \text{MC}_\Lambda,$$

where $\alpha = 0.5$. Applying the LPU law from Eq. (15), obtains

$$\% \sigma^2_{\text{CON}_\Lambda} = \alpha^2 \left( \frac{\text{EXP}_\Lambda}{\text{CON}_\Lambda} \right)^2 \% \sigma^2_{\text{EXP}_\Lambda} + (1 - \alpha)^2 \left( \frac{\text{MC}_\Lambda}{\text{CON}_\Lambda} \right)^2 \% \sigma^2_{\text{MC}_\Lambda} + (\% \sigma_B)^2. \quad (19)$$

$\% \sigma_B$ is an additional component of uncertainty in CON$_\Lambda$ due to the possible bias in the average of the results of experimental and Monte Carlo methods, and is modeled by a Type B rectangular distribution, bounded by EXP$_\Lambda$ and MC$_\Lambda$. The bias $B$ is assumed to be equal to zero, with standard uncertainty given by $\% \sigma_B = 100 |\text{EXP}_\Lambda - \text{MC}_\Lambda| / (2 \sqrt{3} \text{CON}_\Lambda)$. For the various seed models presented in this protocol, $\% \sigma_B$ varies from 0.4% to 1.5%, depending on the magnitude of the discrepancy between Monte Carlo and TLD results. Assuming $\% \sigma_{\text{EXP}_\Lambda} = 8.7\%$ along with model-specific $\% \sigma_{\text{MC}_\Lambda}$ and $\% \sigma_B$ values, $\% \sigma_{\text{CON}_\Lambda}$ varies from 4.6% to 5.0%. Thus for the purposes of practical uncertainty assessment, a model independent $\% \sigma_{\text{CON}_\Lambda}$ value of 4.8% is recommended.
As common in the field of metrology, future changes and improvements to the NIST WAFAC air-kerma strength measurement system and other calibration standards are expected, and may somewhat impact dose rate constant values. For example, the international metrology system has recently revised the $^{60}$Co air-kerma standard for teletherapy beams. Consequently, NIST has revised its $^{60}$Co air-kerma standard effective July 1, 2003 by about 1% due to new, Monte Carlo based wall corrections ($k_{wall}$) for graphite-wall ionization chambers. Changes in the NIST $^{60}$Co air-kerma strength methods from the preceding section, $\sigma_{un}(r)$, will only affect (i) detectors calibrated using either $^{60}$Co beams directly, or (ii) detectors calibrated using high-energy photon beams (e.g., 6 MV) calibrated with ionization chambers which were themselves calibrated using the $^{60}$Co standard. As long as these changes are small in comparison to the aforementioned value of 8.7%, the clinical medical physicist need not be immediately concerned.

3. $g(r)$ uncertainty

For the sources considered in this report, except for the NASI model MED3631-A/M $^{125}$I source, the Monte Carlo-derived values, $MCg(r)$, were adopted as the consensus dataset for radial dose function, $CONg(r)$. For this one seed, the $CONg(r)$ values were based on diode measurements by Li et al.$^{48}$ Therefore, an uncertainty analysis of both $MCg(r)$ and $EXPg(r)$ is presented separately.

Since $MCg(r)$ is a relative quantity that is not combined with experimental results which are used only for validation, it is therefore assumed that experimental data do not contribute to the uncertainty of $CONg(r)$. Again, three sources of uncertainty are considered: statistical variations, cross-section uncertainty, and geometric uncertainties. Using the methods from the preceding section, $\%\sigma_{g(r)}[\mu]$ is 1.8%, 0.8%, and 0% at 0.1, 0.5, and 1.0 cm, respectively. As distance increases from 2 to 5 cm, $\%\sigma_{g(r)}[\mu]$ progressively increases from 0.2% to 4.6%, respectively. $\%\sigma_{g(r)}[geo]$ is again estimated from Williamson's DraxImage and Rivard's MED3631-A/M data assuming a rectangular distribution bounded by the extreme values. For the geometric variations described above, these data show a relative $g(r)$ range of about 8% for $r<0.25$ cm, and 2% at 0.5 cm, corresponding to a $\%\sigma_{g(r)}[geo]$ of 2.3% and 0.6% for $r<0.25$ and 0.5 cm, respectively. Conservatively rounding these values to 3% and 1%, respectively, $\%\sigma_{g(r)}$ varies from 3.5% at 0.1 cm, 0% at 1 cm, and 4.6% at 5 cm.

In this analysis, the uncertainty is zero at $r=0$, and follows from the definition of $g(r)$ which specifies that $g(1)$ is the ratio of the same two identical numbers. In the general uncertainty propagation formula, this is equivalent to assuming the correlation coefficient is equal to -1 when $r=1$ cm. The correlation coefficient is the covariance divided by the product of the standard deviations, so if one sets the correlation coefficient equal to -1, then Cov($x,y$) = $-\sigma_x\sigma_y$. Letting $y=x$, analogous to our case of $D(r)=D(1)$, Cov($x,x$) = $-\sigma_x^2$. Substitution in the propagation of uncertainties formula yields $\sigma_{D(r),D(1)}=0$ when $r\neq 1$ cm. This appears to be a conservative assumption since correlation of statistical variance between two Monte Carlo-derived variables generally reduces the total variance of any algebraic combination of such variables.

Determination of $EXPg(r)$ values using a diode is afflicted by measurement uncertainties similar to those in TLD measurement of $EXP\Lambda$. In measurements by Li et al.,$^{48}$ diode readings were corrected for energy response variations through the range of measurement distances (0.5 cm to 7 cm) as well as volume averaging of diode active detector element.$^{49}$ Measurement uncertainties included (i) a diode detector positioning uncertainty of 0.1 mm, (ii) electrometer leakage current correction uncertainty, and (iii) measurement reproducibility. Inspection of these uncertainties indicates that at short distances ($r<1$ cm), positioning uncertainties contributed the most to the overall uncertainties; whereas at large distances the electrometer leakage current dominated. The overall measurement uncertainties were calculated by combining all three standard uncertainty components in quadrature, and normalizing to 1 cm as discussed above. In summary, the combined standard uncertainty of $EXPg(r)$ was 5.5% at $r=0.5$ cm, approximately 3% over the distance range of 1.5 to 4 cm, and gradually rose to 15% at $r=7$ cm.

4. Anisotropy function uncertainty

Currently, sufficient data are not available in the literature to provide a similarly comprehensive uncertainty analysis for Monte Carlo-derived 1D and 2D anisotropy functions. More research is needed, particularly in the area of identifying geometric parameters to which $F(r,\theta)$ is sensitive, such as end weld configuration and thickness, capsule wall thickness, internal component alignment uncertainties, and deviation of internal structures with sharp edges from their idealized geometries.

5. Total uncertainty of transverse-plane dose-rate calculations

As Eqs. (10) and (11) demonstrate, absolute dose rate is proportional to air-kerma strength, consensus dose-rate constant, consensus anisotropy function, and consensus radial dose function. Thus, ignoring uncertainties in anisotropy function,

$$\%\sigma_{D(r)} = \sqrt{\%\sigma_{SK}^2 + \%\sigma_{CON\Lambda}^2 + \%\sigma_{CONg(r)}^2}.$$  (20)

Assuming that the unexpanded uncertainty, $\%\sigma_{SK}$, of vendor-supplied calibrations is probably no better than 3%, Eq. (20) leads to the conclusion that the total dose-calculation uncertainties are 6.7%, 5.7%, and 7.3% at 0.1, 1, and 5 cm, respectively. As the combined uncertainties associated with the consensus dosimetric parameters probably exceed 5%, clinical physicists should meticulously verify and assign the air-kerma strength values associated with clinical seeds to ensure that $\%\sigma_{SK}$ does not dominate the total uncertainty of the dose calculation. Note that this assessment does not account for uncertainties in evaluating the
effects of anisotropy; the analysis presented herein is neither complete nor rigorous: the AAPM supports further research in the area of brachytherapy dose-calculation uncertainties.

V. RECOMMENDED METHODOLOGY TO OBTAIN BRACHYTHERAPY DOSIMETRY PARAMETERS

In this section, the AAPM recommends a list of methodological details that should be described in brachytherapy dosimetry publications based upon either experimental or theoretical methods, along with more prescriptive guidelines on performing such studies. The list of key details documented in this report for each study is reviewed later. To better appreciate results from a particular dosimetric measurement and its uncertainties, the reader is referred to a listing of parameters needed to assess data for TLD measurements. Unfortunately, this level of description was not realized in many of the papers cited. When key data or methodological details were missing from a published paper, the author was contacted and asked to provide the missing information.

A. General recommendations

Since publication of TG-43, the LIBD has published guidelines on dosimetric prerequisites for low-energy photon-emitting interstitial brachytherapy sources. The aim of those recommendations was to assure that multiple dosimetry studies, each subjected to the rigors of the peer-review process, were available for each source model. However, that publication gave few technical guidelines to investigators publishing reference-quality dose-rate distributions derived from measurements or radiation transport calculations. Based on the LIBD experience of analyzing dosimetry datasets, more detailed recommendations on dosimetry methodology and data analysis are presented in this section. These recommendations are intended to define minimum requirements for future source dosimetry studies so that the accuracy and consistency of the consensus datasets may be improved.

B. Preparation of dosimetry parameters

Dosimetric parameters should be tabulated for both 1D and 2D dose-calculation models. This will require the investigator to calculate the geometry function and the radial dose function using both point-source (1D) and line-source (2D) geometry functions (see Sec. III A.3). Consequently, the investigator should always specify the active length used for the 2D line-source geometry function. As previously stated in Sec. III B, Eq. (11) is the recommended formalism for the 1D approximation.

Specification of dosimetry parameters at a few distances or angles will not allow a sufficiently complete or accurate dose reconstruction of the 2D dose distribution adequate for clinical implementation. In many instances, the underlying dose distribution will have high gradients. Inadequate spatial resolution may result in inaccurate interpolation by brachytherapy treatment planning systems, unnecessarily giving rise to dose-delivery errors. Therefore, it is necessary to recommend minimum spatial resolutions and ranges for which these parameters should be specified.

1. Air-kerma strength

For experimental measurement of absolute dose rates to water, at least one source should have direct traceability of to the 1999 NIST WAFAC calibration standard. Other sources used in the experiment should have a precisely transferred air-kerma strength using high-precision transfer devices such as well-characterized well-ionization chambers and secondary standards maintained by the investigator as well as the manufacturer’s laboratories. The investigator using experimental techniques should state the NIST calibration uncertainty in the evaluation of . Use of another source, even the same model, to cross-calibrate dosimeters for the determination of is highly discouraged since uncertainties propagate and hidden errors may exist.

2. Dose-rate constant

The experimental investigator should rigorously control and try to minimize all detector response artifacts such as dose-rate dependence, dose response nonlinearity, energy dependence, volumetric averaging, temporal stability of readings and calibration coefficients, and accuracy of detector positioning both in the source measurement setup and the detector calibration setup. These issues should be discussed in the measurement methodology section of the published paper, and a rigorous uncertainty analysis should also be provided.

Experimentally, is evaluated by taking the ratio of the absolute dose rate, , (the only absolute dose rate required to define TG-43 dosimetry parameters) and the measured air-kerma strength of the source, decayed to the time of dose-rate measurement. Typically 8–10 sources are used, with at least one source having direct traceability to a NIST calibration. At least 15 measurements of are generally performed. For example, multiple measurements of around a single NIST WAFAC-calibrated source could be made by placing multiple TLDs in different quadrants of the transverse-plane.

Monte Carlo radiation transport codes commonly provide direct estimates of absorbed dose or collision kerma per number of histories simulated (or some other internal normalization quantity, e.g., number of disintegrations, proportional to the number of primary photons simulated). Two simulations are necessary: one with the source model embedded in a phantom, yielding estimates of dose at specified points, and a second simulation with the source model positioned within a vacuum or a large air sphere. The dose-rate constant can then be estimated using the following ratio [Eq. (21)] since the numerator and denominator are similarly normalized, and the normalization constant used by the Monte Carlo code is irrelevant.

\[
\Lambda = \frac{d(r_0, \theta_0)}{s_K}. \tag{21}
\]
The parameter \( \dot{d}(r_0, \theta_0) \) is the dose rate per history estimated using Monte Carlo methods at the reference position, and \( s_K \) is the air-kerma strength per history estimated using Monte Carlo methods. Note the lower-case notation used to differentiate the normalized parameter, e.g., dose rate per history (cGy h\(^{-1}\) history\(^{-1}\)) as compared to absolute dose rate (cGy h\(^{-1}\)). Although Monte Carlo studies are potentially free from experimental artifacts such as positioning uncertainties, energy response corrections, and signal-to-noise ratio limitations, such simulations require an accurate and complete geometric model of the source, selection of an appropriate cross-section library, and careful selection of dose tallying (estimation) and variance-reduction strategies. As with experimental studies, Monte Carlo-based dosimetry studies should include a complete uncertainty analysis such as that provided in Sec. IV C.

3. Radial dose function

The minimum distance range over which transverse-plane dose-rate data shall be measured or calculated should be from 0.5 to 7 cm for \(^{125}\)I and from 0.5 to 5 cm for \(^{103}\)Pd. Special attention to accuracy and completeness should be given to the 0.5 cm to 1.5 cm distance range, which is the most critical for accurately calculating dose for typical prostate and other volume implants and for accurately relating absolute dose rates (via the dose-rate constant) to the relative dose distribution. However, accurate dose characterization at shorter distances is critical for some procedures (e.g., episcleral eye plaque therapy) and for estimating hotspots in all source designs with anisotropic photon-fluence distributions may be needed, with 10° resolution elsewhere. For those regions such as near the source ends \( \approx 0° \) or \( \approx 180° \). Angular resolution of a few degrees near the ends may be needed, with 10° resolution elsewhere. For those source designs that are asymmetric about the transverse plane or exhibit internal component shifts that may result in asymmetric dose distributions, \( F(r, \theta) \) should be similarly tabulated, except with \( \theta = 0° \) to 180° with 10° increments.

Because of the increased sampling capabilities using Monte Carlo methods in comparison to experimental methods, investigators using Monte Carlo methods should consider calculating dose rates using much finer grids in high-gradient regions such as near the source ends (e.g., \( \theta \) near 0° or 180°). Angular resolution of a few degrees near the ends may be needed, with 10° resolution elsewhere. For those source designs with anisotropic photon-fluence distributions near the transverse plane, measurements and calculations having higher angular resolution are required to ensure that experimentally determined anisotropy functions are accurately normalized and that air-kerma strength per simulated history for Monte Carlo simulations is accurately calculated.

### 4.2D anisotropy function

When reporting 2D anisotropy function data, at a minimum, \( F(r, \theta) \) should be tabulated at radial distances, \( r = \{0.5, 1, 2, 3, 5, \text{ and } 7 \text{ cm} \} \) for \(^{125}\)I and \( \{0.5, 1, 2, 3, \text{ and } 5 \text{ cm} \} \) for \(^{103}\)Pd, and from \( \theta = 0° \) to 90° with 10° increments for all sources that are symmetric about the transverse plane. To minimize extrapolation errors (see Appendix C), data should be determined over as wide a radial distance range as reasonably possible given the experimental method or calculation technique. To minimize interpolation errors, data should also be obtained such that bilinear interpolation between various \( F(r, \theta) \) data points produce errors less than 2%. When measuring 2D anisotropy function data with sources that are cylindrically symmetric and symmetric about the transverse plane (four identical quadrants), it is recommended that investigators determine relative dose rates a minimum of three times at each position analyzed. For source designs that are asymmetric about the transverse plane or exhibit internal component shifts that may result in asymmetric dose distributions, \( F(r, \theta) \) should be similarly tabulated, except with \( \theta = 0° \) to 180° with 10° increments. Because of the increased sampling capabilities using Monte Carlo methods in comparison to experimental methods, investigators using Monte Carlo methods should consider calculating dose rates using much finer grids in high-gradient regions such as near the source ends (e.g., \( \theta \) near 0° or 180°). Angular resolution of a few degrees near the ends may be needed, with 10° resolution elsewhere. For those source designs with anisotropic photon-fluence distributions near the transverse plane, measurements and calculations having higher angular resolution are required to ensure that experimentally determined anisotropy functions are accurately normalized and that air-kerma strength per simulated history for Monte Carlo simulations is accurately calculated.

### Table XIII. Recommended nuclear data for \(^{125}\)I and \(^{103}\)Pd for brachytherapy dosimetry.

<table>
<thead>
<tr>
<th>(^{125})I (half-life = 59.40±0.01 days)</th>
<th>(^{103})Pd (half-life = 16.991±0.019 days)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Photon energy (keV)</td>
<td>Photon energy (keV)</td>
</tr>
<tr>
<td>27.202</td>
<td>20.074</td>
</tr>
<tr>
<td>27.472</td>
<td>20.216</td>
</tr>
<tr>
<td>30.98</td>
<td>22.72</td>
</tr>
<tr>
<td>31.71</td>
<td>23.18</td>
</tr>
<tr>
<td>35.492</td>
<td>39.75</td>
</tr>
<tr>
<td>294.98</td>
<td>294.98</td>
</tr>
<tr>
<td>357.5</td>
<td>59.40</td>
</tr>
<tr>
<td>497.1</td>
<td>497.1</td>
</tr>
</tbody>
</table>

Weighted mean energy = 28.37 keV Total = 1.476

\(^{125}\)I \( \Gamma_s \) keV = 0.0355 \( \mu \text{Gy} \cdot \text{m}^{-2} \cdot \text{h}^{-1} \cdot \text{Bq}^{-1} \)

Weighted mean energy = 20.74 keV Total = 0.7714

\(^{103}\)Pd \( \Gamma_s \) keV = 0.0361 \( \mu \text{Gy} \cdot \text{m}^{-2} \cdot \text{h}^{-1} \cdot \text{Bq}^{-1} \)
crease in the number of photons per decay.

The spectrum should now be described in terms of five different photon energies. Although the relative number of high-energy photons emitted beyond 10 cm can be clinically relevant and should also be considered for shielding calculations and exposure-control procedures.56

5. 1D anisotropy function

To derive 1D anisotropy function data, a solid-angle weighted-average of the relative dose rates, uncorrected by the geometry function, should be performed over all angles. When examining small radii where \( \theta = 0^\circ \) or \( 180^\circ \) would place the calculation point within the source, the weighting should exclude the capsule/source volume and include only the volume outside the encapsulation. This is easily calculated for radii, \( r \), less than half the capsule length where \( r \sin \theta > r_{\text{cap}} \), where \( r_{\text{cap}} \) is the outer radius of the capsule.

C. Reference data and conditions for brachytherapy dosimetry

1. Radionuclide data

Since publication of the 1995 TG-43 protocol, the half-lives, abundances and energies of photons emitted by unfiltered \( ^{125}\text{I} \) and \( ^{103}\text{Pd} \) sources have been re-evaluated by NIST.52–55 The currently recommended values are presented in Table XIII. These values should be used to interpret future experimental measurements and as source spectra in Monte Carlo calculations. The recommended \( ^{125}\text{I} \) half-life is unchanged from the original TG-43 protocol. Differences between the recommended \( ^{103}\text{Pd} \) half-life and that reported in TG-43 yield differences in the decay corrections exceeding 1% only for decay times \( > 200 \text{ days} \). Of note is that the \( ^{125}\text{I} \) spectrum should now be described in terms of five different photon energies (previously three) with a 5% increase in the number of photons per decay (previously 1.40). The \( ^{103}\text{Pd} \) emission spectrum should now be described in terms of eight discrete photon emissions (previously two) with a 4% decrease in the number of photons per decay (previously 0.8). Although the relative number of high-energy photons emitted by \( ^{103}\text{Pd} \) is low, their contribution to dose at distances beyond 10 cm can be clinically relevant and should also be considered for shielding calculations and exposure-control procedures.56

2. Reference media

Water continues to be the recommended medium for reference dosimetry of interstitial brachytherapy sources. For dosimetry calculations and measurements, it may be necessary to know the composition of various forms of water and air. Pure, degassed water is composed of two parts hydrogen atoms and one part oxygen atoms, with a mass density of 0.998 g cm\(^{-3}\) at 22 °C. Reference conditions for dry air are taken as 22 °C and 101.325 kPa (760 mm Hg) with a mass density of 0.001 196 g cm\(^{-3}\). Since the composition of air may change as a function of relative humidity, Table XIV is provided to account for this effect.57,58 The proportion by weight of water in air of 100% relative humidity varies only between 1% and 2%, for temperatures between 16 °C and 26 °C and pressures between 735 mm Hg and 780 mm Hg. The change in mass density of saturated air is no more than a 1% reduction with respect to that for dry air, over this range of temperatures and pressures. Thus, the mass density will be set at 0.001 20 g cm\(^{-3}\) for both dry and moist air. For Monte Carlo calculations, the recommended relative humidity is 40%, which corresponds to the relative humidity in an air-conditioned environment where measurements should be carried out.

D. Methodological recommendations for experimental dosimetry

Compared to Monte Carlo theorists who may idealize reality by a theoretic construct, the experimental investigator should address the variability that represents the clinical environment. The experimental study should investigate a reasonably large sample of sources received from multiple shipments at different stages of the production stream from the manufacturer.

1. Detector choice

LiF TLD remains the method of choice for the experimental determination of TG-43 dosimetry parameters for low-energy photon-emitting brachytherapy sources.59–63 While a variety of other experimental dosimeters such as diodes, diamond detectors, miniature ionization chambers, plastic scintillators, liquid ionization chambers, polymer gels, radiographic and radiochromic film, and chemical dosimeters have been used for brachytherapy dosimetry,58,49,64–80 their validity for obtaining brachytherapy dosimetry parameters has not yet been convincingly demonstrated for absolute dose-rate measurements near low-energy photon-emitting brachytherapy sources. For dosimetry parameters based on relative measurements, some of these other dosimeters have been successfully used. Diode detectors, in particular, are well established for relative measurements.65,68,70 For \( ^{125}\text{I} \), Li et al. has shown that the relative energy-response correction, although large, is independent of the point of measurement.49 However, validity of the results of absolute and relative dosimetry parameters using these experimental dosimeters (other than LiF TLDs and diodes) remains to be demonstrated through comparison of results with established Monte Carlo calculations.48,49,64–80

### Table XIV. Composition (percent mass) of air as a function of relative humidity at a pressure of 101.325 kPa.

<table>
<thead>
<tr>
<th>Relative humidity (%)</th>
<th>Hydrogen</th>
<th>Carbon</th>
<th>Nitrogen</th>
<th>Oxygen</th>
<th>Argon</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>0.0000</td>
<td>0.0124</td>
<td>75.268</td>
<td>23.178</td>
<td>1.287</td>
</tr>
<tr>
<td>10</td>
<td>0.0181</td>
<td>0.0124</td>
<td>75.4048</td>
<td>23.2841</td>
<td>1.2806</td>
</tr>
<tr>
<td>40</td>
<td>0.0732</td>
<td>0.0123</td>
<td>75.0325</td>
<td>23.6077</td>
<td>1.2743</td>
</tr>
<tr>
<td>60</td>
<td>0.1101</td>
<td>0.0123</td>
<td>74.7837</td>
<td>23.8238</td>
<td>1.2701</td>
</tr>
<tr>
<td>100</td>
<td>0.1842</td>
<td>0.0122</td>
<td>74.2835</td>
<td>24.2585</td>
<td>1.2616</td>
</tr>
</tbody>
</table>

Medical Physics, Vol. 31, No. 3, March 2004
Carlo and experimental techniques using well-characterized $^{125}$I or $^{103}$Pd sources (such as those contained in this protocol). Multiple publications of results in peer-review journals by independent investigators (see the second meaning of “independent studies” in Sec. V F) are desirable to demonstrate independence and consistency. Therefore, use of these experimental dosimeters is an area of future research of significant scientific value. For measuring brachytherapy dosimetry parameters, detectors should have the following properties:

(a) Detectors should have a relatively small active volume such that effects of averaging of high-gradient dose fields over this volume are negligible or are accurately accounted for by correction coefficients.

(b) A well-characterized energy-response function such that differences between the calibration energy and experimentally measured energy are either negligible or may be quantitatively accounted for.

(c) Sufficient precision and reproducibility to permit dose-rate estimation with $1 \sigma$ statistical (Type A) uncertainties $\leq 5\%$, and $1 \sigma$ systematic uncertainties $< 7\%$. For example, TLD statistical uncertainties may be improved through repeated measurement at a given location, and systematic uncertainties may be improved through measuring chip-specific calibration coefficients. Typical statistical and systematic uncertainties for $1 \times 1 \times 1$ mm$^3$ TLD-100 chips are 4% and 7%, respectively, with total combined uncertainties of 7–9%. Therefore, $1 \times 1 \times 1$ mm$^3$ TLD-100 chips are considered a valid detector to perform the aforementioned absolute and relative measurements.

Because none of the experimental dosimeters satisfy the above prerequisites for absolute dose measurement, LiF thermoluminescent dosimetry is currently the method of choice for experimental determination of the dose-rate constant and is the most extensively (but not only) validated methodology for relative dose measurement. Several important issues in TLD dosimetry are discussed in more detail in the following section.

2. Medium and energy response characterization

It is necessary that the measurement medium should also be well characterized. While epoxy-based substitutes for water, such as Solid Water$^{TM}$ by Gammax-RMI or Virtual Water$^{TM}$ by MED-TEC Inc., have liquid–water conversion coefficients that differ from unity by less than 5% for high-energy teletherapy beams, coefficients range from within 5% to 15% from unity for low-energy photon-emitting sources. Recently, the measured calcium concentration of Solid Water$^{TM}$ was found to have deviated from the vendor’s specification by as much as 30%. Therefore, when Solid Water$^{TM}$ is used in experimental dosimetry, the atomic composition of the material used should be measured and correction coefficients based on the measured composition of Solid Water$^{TM}$ should be used. Although Solid Water$^{TM}$ is the most widely used material for TG-43 reference dosimetry, it has several shortcomings. In addition to concerns over the constancy of its composition, Solid Water$^{TM}$ and similar water substitutes require solid-to-liquid water conversion corrections ranging from within 5% to 15% from unity in the 1–5 cm range. Alternative materials need to be researched by future investigators. Because some of the low-Z media such as polystyrene, polymethylmethacrylate, or plastic water (model PW2030 by Computerized Imaging Reference Systems, Inc.) generally have more uniform and better-characterized compositions, these media may be possible candidates for future low-energy photon-emitting brachytherapy dosimetry studies. However, values for their plastic-to-water conversion coefficients, which are expected to be larger than corresponding Solid Water$^{TM}$ corrections, need to be accurately determined for dosimetrically well-characterized source models, such as those covered in this protocol, and validated by independent investigators in peer-reviewed publications.

The relative energy response correction, $E(r)$, is the largest single source of Type B (systematic) uncertainty for TLD and other secondary dosimeters used in brachytherapy dosimetry. It is defined as the ratio of TLD response per unit dose in water medium at position $r$ in the brachytherapy source geometry, to its response per unit dose in the calibration geometry, usually a calibrated $^{60}$Co or 6 MV x-ray beam. In general, $E(r)$ depends on source-to-detector distance, $r$, and may include corrections for volume averaging (influence of dose gradients in the TLD volume), detector self-absorption, medium displacement, and conversion from the measurement medium to liquid water. Most investigators treat $E(r)$ as a distance-independent constant, although when it includes volume-averaging and solid-to-liquid water corrections, as is often the case for Monte Carlo estimates, $E(r)$ varies significantly with distance. This correction can be evaluated by irradiating TLD detectors to a known dose in free space in a calibration low-energy x-ray beam having a spectrum that matches the brachytherapy spectrum of interest. For TLD-100 and liquid-water measurement medium, values ranging from 1.39 to 1.44 for $^{125}$I, relative to 4 MV x rays or $^{60}$Co rays, have been reported. For $^{125}$I, Meigooni et al. and Reft have shown that $E(r)$ values inferred from in-air measurements depend on TLD size. Since free-air measurements relate TLD reading to dose in a void left by removing the chip, a replacement correction (2%–5%), is needed to correct for the phantom material displaced by the detector. However, precise measurement of $E(r)$ is difficult because (i) photons from the low-energy tail of the Bremsstrahlung spectrum bias the measurements to an unknown extent, (ii) the limited precision of TLD readout, and (iii) the relatively large uncertainty of ion chamber dosimetry in this energy range. Recent authors have assigned an uncertainty of 5% to $E(r)$. An alternative to the experimental approach is to calculate $E(r)$ directly by Monte Carlo simulation. Although volume-averaging, displacement and detector self-attenuation corrections can be easily included, the method assumes that TLD response is proportional to energy imparted to the detector (intrinsic linearity), an assumption which has been questioned for some TLD phosphors and annealing and glow-curve analysis techniques.
chips using Cameron annealing and readout techniques, the evidence for intrinsic linearity is controversial. Das et al. compared the Monte Carlo and the experimental free-air x-ray beam approaches. Their measured relative responses (1.42–1.48) were in good agreement (relative to stated 4% experimental precision) with measurements reported by other investigators and with their own Monte Carlo calculations. However, a recent paper by Davis et al. concludes the opposite, that the measured TLD-100 energy response correction is underestimated by Monte Carlo calculations by 10% to 5% in the 24 to 47 keV energy range. Their measured $E(r)$ values, which have stated uncertainty of 0.6%, are about 10% larger than previously reported measurements, having values ranging from 1.58 to 1.61 in the $^{103}$Pd–$^{125}$I energy range.

In utilizing measured or Monte Carlo $E(r)$ estimates published by others, LIBD recommends that TLD experimentalists confirm that the associated measurement methodology matches their dosimetry technique with regard to TLD detector type and size, annealing and readout technique, and megavoltage beam calibration technique. The latter requires accounting for differences in calibration phantom material and dose-specification media used by the experimentalist and assumed by the selected $E(r)$ estimate. The experimentalist should confirm the appropriate volume averaging, displacement, and self-absorption corrections regardless of whether they are included in $E(r)$ or applied separately. Finally, further research is needed to resolve the discrepancy between published $E(r)$ values, to identify the appropriate role for transport calculations in TLD dosimetry, and to reduce the large uncertainty associated with relative energy-response corrections.

3. Specification of measurement methodology

The experimental investigator should describe the following important features of the measurement materials and methods to permit assessment of the results:

1. description of the external and internal source geometry,
2. brachytherapy source irradiation geometry, orientation, and irradiation timeline,
3. radiation detector calibration technique (including protocol from which the technique is derived) and energy response function, $E(r)$,
4. radiation detector (dimensions, model No., and vendor) and readout system (e.g., electrometer unit model No. and settings, or TLD readout unit model No., vendor, time-temperature profiles, and annealing program),
5. measurement phantom (composition, mass density, dimensions, model No., and vendor),
6. phantom dimensions and use of backscatter (at least 5 cm backscatter is recommended for $^{125}$I and $^{103}$Pd dosimetry measurements),
7. estimation of the impact of volume averaging on the results at all detector positions,
8. number of repeated readings at each position, the number of different sources used, and the standard deviation of the repeated readings,
9. NIST $S_K$ value and uncertainty used for the measured source(s), and
10. uncertainty analysis section assessing statistical and systematic uncertainties and their cumulative impact.

E. Methodological recommendations for Monte Carlo-based dosimetry

Monte Carlo codes used to model photon transport for brachytherapy dose calculation should be able to support detailed 3D modeling of source geometry and appropriate dose-estimation techniques. In addition, they should be based upon modern cross-section libraries and a sufficiently complete model of photon scattering, absorption, and secondary photon creation. Codes that have been widely used for interstitial brachytherapy dosimetry include EGS, MCNP, and Williamson’s PTRAN code. These codes have been widely benchmarked against experimental measurements or each other, so that their appropriate operating parameters and limitations can be considered to be well understood. In general, the AAPM recommends Monte Carlo investigators utilize such well-benchmarked codes for brachytherapy dosimetry studies intended to produce reference-quality dose-rate distributions for clinical use. However, regardless of the transport code chosen and its pedigree, all investigators should assure themselves that they are able to reproduce previously published dose distributions for at least one widely used brachytherapy source model. This exercise should be repeated whenever new features of the code are explored, upon installing a new code version, or as part of orienting a new user. Other radiation transport codes, including Monte Carlo codes not previously used in brachytherapy dosimetry, should be more rigorously tested and documented in the peer-reviewed literature before proposing to use their results clinically. This is especially true for other types of transport equation solutions, including multigroup Monte Carlo, discrete ordinates methods, and integral transport solutions that have been proposed for brachytherapy dosimetry.

Due to the short range of the secondary electrons produced by interactions from photons emitted by the radionuclides covered in this protocol, electron transport is not required and collision kerma closely approximates absorbed dose. Since the investigator performing Monte Carlo analysis can control many features of the transport calculations, it is imperative that the salient details be described in publications presenting Monte Carlo-derived brachytherapy dosimetry data. For instance, the collisional physics model should be described. The standard model used by experienced Monte Carlo users includes incoherent scattering corrected for electron binding by means of the incoherent scattering factor, coherent scattering derived by applying the atomic form factor to the Thompson cross section, and explicit simulation of characteristic x-ray emission following photo-electric absorption in medium- and high-atomic number media. For sources containing Ag or Pd, it is imperative that, if characteristic x-ray production is not explicitly simulated, the primary source spectrum be appropriately augmented to include their presence.

Medical Physics, Vol. 31, No. 3, March 2004
1. Specification of Monte Carlo calculation methodology

A list of key features that should be specified by the investigator in the publication follows:

1. radiation transport code name, version number, and major options if any,
2. cross-section library name, version number, and customizations performed if any,
3. radiation spectrum of the source (consider Table XIII in Sec. V C.1),
4. manner in which dose-to-water and air-kerma strength are calculated: name of estimator or tally, whether or not transport was performed in air and how attenuation correction coefficients were applied, and how suppression of contaminant x-ray production for $\hat{k}_{\beta}(d)$ calculations was performed to be compliant with the NIST $S_{X,999}$ standard,
5. source geometry, phantom geometry, and sampling space within the phantom,
6. composition and mass density of the materials used in the brachytherapy source,
7. composition and mass density of the phantom media,
8. physical distribution of the radioisotope within the source, and
9. uncertainty analysis section assessing statistical and systematic uncertainties and their cumulative impact.

2. Good practice for Monte Carlo calculations

For calculating brachytherapy dosimetry parameters, the following requirements should be adhered to:

1. Primary dosimetry calculations should be performed in a 30 cm diameter liquid water phantom, but calculations in Solid Water may also be performed to supplement experimental results, e.g., calculation of $E(r)$, performed in Solid Water or other solid water substitutes. Typical calculations will produce dosimetry results extending out to $r \sim 10$ cm, with at least 5 cm of backscatter material for $^{125}$I and $^{103}$Pd dosimetry calculations.
2. Enough histories should be calculated to ensure that dosimetry results have a $1\sigma$ ($k = 1$, 67% confidence index) $\leq 2\%$ at $r \leq 5$ cm, and that $\hat{k}_{\beta}(d)$ calculations for derivation of $s_X$ have $1\sigma \leq 1\%$ at the point of interest.
3. Modern, post-1980 cross-section libraries should be used, preferably those equivalent to the current NIST XCOM database such as DLC-146 or EPDL97. Exclude or appropriately modify older cross-section libraries based on Storm and Israel data. Note that EGS4, EGSnrc, and MCNP all currently require modification or replacement of their default photoionization cross sections to meet this requirement. Furthermore, moist air best-describes experimental conditions in comparison to dry air (see Sec. V C.2), and mass-energy absorption coefficients for moist air are recommended to minimize systematic uncertainties.
4. Manufacturer-reported source dimensions and compositions of encapsulation and internal components should be verified through the use of physical measurements, transmission radiography, and autoradiography. Just as the TLD experimentalist should measure an appropriate sample of sources, the Monte Carlo investigator should quantify the geometric variations in a sample of similar size.
5. The impact of volume-averaging artifacts should be limited to $<1\%$ through the appropriate choice of estimators (tallies) and scoring voxels if used.
6. Calculations of $d(r, \theta)$ to derive $F(r, \theta)$ should include high-resolution sampling in high-gradient regions such as near the source ends or in regions where internal source shielding causes abrupt changes in $d(r, \theta)$ and subsequently $F(r, \theta)$.
7. $k(d)$ should be modeled as a function of polar angle for $s_X$ simulation and $\Lambda$ derivation. Williamson has shown that for some sources, detectors with large angular sampling volumes (such as the NIST WAFAC) will have a significantly different response than point-kerma detectors positioned on the transverse-plane (see Appendix B.2.2 for greater detail). When the radioactivity is dispersed within or on the surface of a high-density core with sharp corners and edges, it may be necessary to simulate, if only approximately, the WAFAC geometry (dimensions and composition) to permit investigators the opportunity to directly compare Monte Carlo calculations of $\Lambda$ with NIST-based measurements of $\Lambda$.
8. Point source modeling is unacceptable. Mechanical mobility of the internal source structures, which has the potential to significantly affect the dose distribution, should be considered by the Monte Carlo investigator in developing both the geometric model of the source and the uncertainty budget.

F. Publication of dosimetry results

Previous AAPM recommendations stated that dosimetry results should be published preceding clinical implementation. However, the journal Medical Physics established a “seed policy” in 2001 that, in effect, limits printing of articles to Technical Notes unless they contain significant new science. In order to comply with this restriction imposed by the journal, the AAPM will accept technical notes with limited details as acceptable, provided the full details as listed above are available to the committee at the time of evaluation. This policy in no way prevents publication of the article in other journals, as other scientific journals of interest to medical physicists are appropriate venues for publication of these dosimetry parameters.

In a 1998 report, the AAPM recommended that dosimetry results be published by independent investigators, but did not offer a strict definition of what this independence entails. The spirit of the initial recommendation was to prompt publication of multiple studies to assess all the TG-43 brachytherapy dosimetry parameters, e.g., $\Lambda$, $g(r)$, $F(r, \theta)$, and $\phi(r)$. Through determining the consensus datasets for the brachytherapy sources evaluated in this protocol, a rigorous definition of the “Independence Policy” was adopted. There...
are two aspects of this policy, and both shall be met for full compliance.

The first meaning of “independent studies” is that they are performed, written, and published by investigators who are affiliated with institutions independent of the source vendor and who have no major conflicts-of-interest with that vendor.

The second meaning of “independent studies” is that they are scientifically independent of one another, i.e., they represent independent and distinct estimations of the same quantities. In the case of two measurement-based studies, this will usually mean that two different investigators have used their own methodologies for measuring λ and sampling the relative dose distribution, as TLD dosimetry is highly technique and investigator dependent. In the case of an empirical study and a Monte Carlo study, if properly executed, they will yield scientifically independent estimates of the TG-43 parameters. Thus, so long as the two studies are successfully scrutinized by the peer-review process and satisfy the AAPM scientific requirements, the empirical and Monte Carlo investigator author lists can overlap or even be identical. It is permissible to publish the Monte Carlo and measured estimates in the same paper so long as the two datasets are independently tabulated. In this context, “Not independent” means that the one study is used to modify the outcomes and methods of the other to improve agreement between the two datasets in a manner that is not scientifically justified.

When possible, the authors should cite previous publications where the measurement system or techniques were first described, and illustrate only the key features. It does not benefit either the reader or the journal in question to continually restate the definition of TG-43 parameters or their formalism. Simply citing this protocol or the original TG-43 publication will suffice.

VI. CLINICAL IMPLEMENTATION

Dose distributions in and around clinical interstitial implants are calculated using computerized radiotherapy treatment planning (RTP) systems. For sources with radio-opaque markers, the 3D coordinates of the centers (or the two ends) of the markers in implanted sources are determined using multiple-view radiographs or CT scans. The dose-rate contributions from each source at the points of interest are calculated using a one-dimensional or two-dimensional dose-calculation algorithm. These contributions are then summed to determine the total dose rate. This procedure assumes that there are no source-to-source shielding effects, that all tissues in and around the implant are water equivalent, and that the scattering volume within the patient is equivalent to that used in the consensus datasets. The term equivalent in this context means at least 5 cm of water-equivalent material surrounds the point of calculation. Many RTP systems are available commercially and use a variety of methods to calculate clinical dose-rate distributions. Some of the RTP systems use the single-source dosimetry data in a tabular form as input, whereas others represent the data by means of a mathematical formula that requires input of certain coefficients. Some use the TG-43 dose-calculation formalism and others do not. In this section, procedures for clinical implementation of the updated dosimetry parameters recommended above are presented.

The medical physicist is reminded that before adopting the recommendations presented in this report, the physicist should implement the dose-calculation data and technique recommended by this report on his/her treatment planning system and quantitatively assess the influence of this action on dose delivery. This is best done by comparing the dose distribution for typical implants based on the revised dose-calculation procedure with those based upon the currently implemented algorithm for the same seed locations, source strengths, and dose-calculation grid. The potential impact of these dose-calculation modifications on dose delivery relative to the current dose-calculation technique should be discussed with the appropriate radiation oncologist before clinically implementing the recommendations of this report. Finally, the comparison of old and new dose-calculation algorithms for the same seed input data, and the resultant decisions that may impact clinical dose delivery, should be documented for future reference and for regulatory purposes.

A. Dose-calculation formalism

For this work, RTP systems are divided into those that comply fully with the TG-43 formalism, and those that do not. Full compliance is defined here as the use of Eq. (1) or one of its two approximations, given in Eqs. (10) and (11). Full compliance also requires the use of the dose-rate constant, appropriate values of the radial dose function, and the 1D or 2D anisotropy functions that are provided in this protocol.

For RTP systems that use the TG-43 dose-calculation formalism and permit customer input of dosimetry parameters, one should enter (or verify the correct entry of) the recommended parameters, and check the accuracy of the dose calculation algorithm. The tabulated data provided in this protocol should be used with such systems. In other cases, coefficients in an equation, e.g., third- to fifth-order polynomial fits, describing the TG-43 parameters may be required. In these cases, the RTP-specific model or formula should be fit to the data provided by this protocol. For example, for systems that require a third-order (or higher) polynomial fit of the radial dose function, the clinical physicist is responsible for obtaining the best-fit coefficients by fitting the polynomial equation to appropriate \( g_X(r) \) data from this protocol.

Before implementing the dose-calculation model, it is necessary to evaluate the quality of the parametric fit. Deviation of the fitted data from those recommended in this protocol should be less than \( \pm 2\% \). This will yield a dose-rate calculation accuracy of \( \pm 2\% \) over the distance range of interest. The medical physicist shall take responsibility for verifying the accuracy of dosimetry data, whether the manufacturer or the user actually enters the data.

Some RTP systems do not use the TG-43 dose-calculation
algorithm and perform calculations using methods not based upon Eqs. (1), (10), or (11). In most cases, one can devise a method to force the algorithm to generate the single-source dose-rate distributions recommended here by using modified values for the dosimetry parameters required by the RTP system. This conversion should be performed with care. As with RTP systems based on the TG-43 dose calculation formalism, one should assure that the RTP system is generating correct single-source dose-rate data by creating a single-source treatment plan with the modified parameters before clinical use. Meigooni et al. have described an example of this approach. The methods used to arrive at modified data, as well as records of the evaluation of the RTP system, should be documented carefully and retained for use following installation of upgrades and for inspection by regulatory authorities. Extreme caution should be exercised whenever parameters should be entered or displayed that have units that do not match the units on documentation printed by the RTP system or displayed on its monitor. Procedures should be developed and documented to describe exactly how the modified data and parameters are related to the non-TG-43 parameters assumed by the RTP system. These procedures should address both clinical treatment planning practices and chart-checking procedures. Ratios of the unconventional units to the conventional units should be supplied, to facilitate review of the planning method. Because this approach is prone to errors in implementation or interpretation, this method should be used as the last resort. The AAPM recommends using RTP systems that comply fully with the TG-43 formalism, whenever possible.

### B. Acceptance testing and commissioning

Before a new RTP system or a new source model on an established RTP system is used for patient treatment planning, thorough acceptance testing and commissioning shall be carried out. The user should document the results of these tests both for later reference, and for compliance with applicable regulations. As a minimum, calculations of the dose-rate distribution shall be performed for a single source of each type to be used clinically. The recommendations of the AAPM (TG-40, TG-53, and TG-56) should be followed.  

The dose rates calculated by the RTP system from a single source should be compared with the dose-rate distribution derived from the tabulated parameters and equations presented in this protocol. The user shall compare the RTP system calculations with the dose-rate distributions derived from the appropriate 1D or 2D data tables from this protocol. To facilitate this comparison, Table XV presents the transverse-plane dose rates (incorporating the 1D anisotropy function), derived from Eq. (11) using the recommended data, as a function of distance for the brachytherapy sources included in this protocol. As has been recommended previously by the AAPM, this comparison should yield agreement within ±2% over all angles and over the range of radial distances commissioned.

The user should determine the range of distances from the source over which the RTP calculations meet this recommended level of accuracy. Use of the RTP system should be limited to this range. If deviations between calculated results and the published data (such as that recommended in Table XV) exceed ±2%, the deficiencies of the RTP system should be documented and further investigated by the user. This is especially important for RTP systems that fit a model to published data, because such models are prone to large errors outside the range of the reference data. In the high-dose-gradient regions close to a source, particularly near the ends of a source, the acceptable error may need to be larger. These deficiencies should be considered when evaluating treatment plans, and when considering the purchase of an RTP system.

To perform comparisons at the recommended level of precision, numerical point dose rates calculated by the RTP system, rather than measured diameters of plotted isodose contours, should be used. The user should evaluate any deviations from the recommended data, taking into consideration the uncertainty of calculations at very small distances. The calculation matrix should be adjusted to a value appropriate for the high gradients near a source. For low-energy photon-emitting sources, grid spacing should not exceed 1 \( \times 1 \times 1 \text{ mm}^3 \); this size generally represents a reasonable compromise between calculation speed and accuracy.

Isodose curves should be generated as part of the commissioning and continuing quality assurance procedures, but should be viewed as a test of the spatial accuracy of the

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**Table XV.** Dose rates (cGy·h\(^{-1} \cdot \text{U}^{-1}\)) as a function of distance for 8 brachytherapy sources using the 1D dosimetry formalism of Eq. (11) with interpolation for \( g_L(r) \) and \( \phi_{\text{ref}}(r) \).

<table>
<thead>
<tr>
<th>( r ) (cm)</th>
<th>Amersham model 6702</th>
<th>Amersham model 6711</th>
<th>Best model 2301</th>
<th>NASI model MED3631-A/M</th>
<th>Bebig model IS-506</th>
<th>Imagyn model IS-12501</th>
<th>Theragenics model 200</th>
<th>NASI model MED3633</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.5</td>
<td>4.119</td>
<td>3.937</td>
<td>3.813</td>
<td>4.112</td>
<td>3.922</td>
<td>3.426</td>
<td>3.014</td>
<td>3.184</td>
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<tr>
<td>1.0</td>
<td>0.995</td>
<td>0.911</td>
<td>0.962</td>
<td>0.986</td>
<td>0.950</td>
<td>0.815</td>
<td>0.587</td>
<td>0.626</td>
</tr>
<tr>
<td>1.5</td>
<td>0.413</td>
<td>0.368</td>
<td>0.413</td>
<td>0.420</td>
<td>0.398</td>
<td>0.334</td>
<td>0.199</td>
<td>0.215</td>
</tr>
<tr>
<td>2.0</td>
<td>0.213</td>
<td>0.186</td>
<td>0.220</td>
<td>0.207</td>
<td>0.205</td>
<td>0.169</td>
<td>0.0837</td>
<td>0.0914</td>
</tr>
<tr>
<td>3.0</td>
<td>0.0768</td>
<td>0.0643</td>
<td>0.0783</td>
<td>0.0746</td>
<td>0.0733</td>
<td>0.0582</td>
<td>0.0206</td>
<td>0.0227</td>
</tr>
<tr>
<td>4.0</td>
<td>0.0344</td>
<td>0.0284</td>
<td>0.0347</td>
<td>0.0325</td>
<td>0.0323</td>
<td>0.0246</td>
<td>0.00634</td>
<td>0.00697</td>
</tr>
<tr>
<td>5.0</td>
<td>0.0169</td>
<td>0.0134</td>
<td>0.0171</td>
<td>0.0157</td>
<td>0.0157</td>
<td>0.0118</td>
<td>0.00221</td>
<td>0.00247</td>
</tr>
<tr>
<td>6.0</td>
<td>0.00890</td>
<td>0.00688</td>
<td>0.00908</td>
<td>0.00811</td>
<td>0.00840</td>
<td>0.00592</td>
<td>0.000846</td>
<td>0.000933</td>
</tr>
<tr>
<td>7.0</td>
<td>0.00490</td>
<td>0.00373</td>
<td>0.00506</td>
<td>0.00429</td>
<td>0.00459</td>
<td>0.00328</td>
<td>0.000342</td>
<td>0.000364</td>
</tr>
</tbody>
</table>
graphic dose display function of the RTP system, rather than a definitive test of the underlying dose-calculation algorithm. Because comparisons should include both point dose-rate calculations and the placement of isodose lines, the user should also ensure that the RTP system and its graphical output devices cause isodose curves to appear in the correct locations relative to corresponding point calculations.

C. Source calibrations

For calibrating radioactive sources, the AAPM has previously recommended that users not rely on the manufacturer’s calibrations, but instead confirm the accuracy of source strength certificates themselves by making independent measurements of source-strength that are secondarily traceable to the primary standard maintained at NIST. For patient treatments, AAPM further recommended that all clinically used sources bear calibrations that are secondarily traceable to the primary standard. AAPM defines “direct traceability,” “secondary traceability,” and “secondary traceability with statistical inference” as follows:

“Direct traceability is established when either a source or a transfer instrument (e.g., well chamber) is calibrated against a national standard at an ADCL or at NIST itself.”

“Secondary traceability is established when the source is calibrated by comparison with the same radionuclide and design that has a directly traceable calibration or by a transfer instrument that bears a directly traceable calibration.”

“Secondary traceability by statistical inference is established when a source is one of a group of sources of which a suitable random sample has direct or secondary traceability.”

This protocol, in accord with the previously published AAPM guidance (TG-56, TG-40), also recommends that all sources implanted into patients have measurements based upon secondary traceability. Normally, vendors should be expected to provide calibration certificates that document secondary traceability to NIST for their sources. Each institution should maintain a means for verifying vendor calibrations by air-kerma strength measurements with secondary traceability. Source sampling and instrument quality assurance guidelines are documented in TG-56. Source strength verification with secondary traceability can be achieved either by means of a chamber bearing a calibration that is directly traceable to the appropriate national standard, or by comparison to a source of the same model having a calibration that is directly traceable to the national standard. These methods are described in the following section.

1. Secondarily traceable calibrations at the institution using a transfer instrument

For brachytherapy sources, calibrating sources with secondary traceability is best done with a well-type ionization chamber having an ADCL-assigned, directly traceable calibration coefficient determined for the source model to be used. TG-56 recommends returning the chamber to the ADCL at intervals of two years for recalibration.

2. Secondarily traceable calibrations at the institution by source intercomparison

When NIST or an ADCL provides an air-kerma strength value for a given source, that source is then said to have a directly traceable calibration. The user can then use this source to calibrate his/her transfer instrument, such as a well chamber. The well chamber in this situation is said to have a calibration coefficient bearing secondary traceability. To accomplish this, the user may obtain a source from a vendor, send it to NIST or an ADCL and obtain an air-kerma strength value for that source. The user can then use this source to calibrate his or her well chamber. The well chamber can then be used to confirm the vendor-stated source strengths of other sources of the same model before they are used clinically.

If the chamber is calibrated by the ADCL, the calibration coefficient is directly traceable. If the calibrated source method is used, the user is responsible for transferring the calibration to his or her instrument. Regardless of which method is used, the well chamber should be checked for constancy on a regular basis using a long-lived source such as $^{137}$Cs. The AAPM has recommended that a constancy check be performed at each use, and that the well chamber exhibit constancy to within $\pm 2\%$. For the calibrated chamber or the calibrated source approach, the total expanded uncertainty ($2\sigma = 95\%$ confidence level) obtained by adding in quadrature the uncertainties of instrument or source calibration at the ADCL (typically 2.4% including the uncertainty at NIST). It is emphasized that the precision of measurement in the well chambers is better than this (generally within $\pm 0.5\%$). The typical total, expanded uncertainty at the user facility using a source transfer to a chamber is typically 3.0%. This is the maximum uncertainty that is relevant for secondarily traceable calibration. Any additional steps in the intercomparison process will increase the total uncertainty and thus will not meet the minimum standard of quality recommended in this protocol. The user is further warned that under no circumstances should a vendor or user calibration be used as a basis of institutional verification calibration.

Finally, it is important not to confuse a source bearing a calibration with direct or secondary traceability with a “calibrated source” obtained from the source manufacturer. Use of a source calibrated by a manufacturer is not an acceptable alternative for providing in-house calibrations with traceability to NIST or an ADCL.
GLOSSARY OF SYMBOLS AND TERMS

AAPM American Association of Physicists in Medicine
ADCL AAPM-Accredited Dosimetry Calibration Laboratory
$\beta$ Angle subtended by $P(r, \theta)$ and the two ends of the active length. As used in the line source approximation, $\beta$ has units of radians.

COMS Collaborative Ocular Melanoma Study of episceral eye plaque therapy versus enucleation trial.

d Distance to the point of measurement from the source center in its transverse plane. Typically measured in-air or in-vacuo. Units of cm.

$\hat{d}(r_0, \theta_0)$ The dose rate per history estimated using Monte Carlo methods at the reference position.

$\hat{D}(r, \theta)$ Dose rate in water at $P(r, \theta)$. The dose rate is generally specified with units cGy h$^{-1}$ and the reference dose rate, $\hat{D}(r_0, \theta_0)$, is specified at $P(r_0, \theta_0)$ with units of cGy h$^{-1}$.

$\delta$ Energy cutoff parameter used for air-kerma rate evaluation, which is 5 keV for this protocol.

F($r, \theta$) 2D anisotropy function describing the ratio of dose rate at radius $r$ and angle $\theta$ around the source, relative to the dose rate at $r_0 = 1$ cm and $\theta_0 = 90^\circ$ when removing geometry function effects. Dimensionless units.

$G_X(r, \theta)$ Geometry function approximating the influence of the radionuclide physical distribution on the dose distribution. $G_X(r, \theta)$ may be calculated by Monte Carlo simulation or by the following:

$G_p(r, \theta) = r^{-2}$ point-source approximation,

$G_L(r, \theta) = \begin{cases} \frac{\beta}{L r \sin \theta} & \text{if } \theta \neq 0^\circ \\ (r^2 - L^2/4)^{-1} & \text{if } \theta = 0^\circ \end{cases}$ line-source approximation,

with units of cm$^{-2}$.

$g(r)$ Radial dose function describing the dose rate at distance $r$ from the source relative to the dose rate at $r_0 = 1$ cm. Dimensionless units.

$g_L(r)$ Radial dose function, determined under the assumption that the source can be represented as a line segment. Dimensionless units.

$g_p(r)$ Radial dose function, determined under the assumption that the source can be represented as a point. Dimensionless units.

$\text{CON}$ Radial dose function derived from consensus dataset. Dimensionless units.

$\dot{k}_\beta(d)$ Air-kerma rate per history in vacuo estimated using Monte Carlo methods, due to photons of energy greater than $\beta$.

$\dot{K}_\delta(d)$ Air-kerma rate in vacuo due to photons of energy greater than $\delta$, with units of cGy h$^{-1}$.

$\Lambda$ Dose-rate constant in water, with units of $\mu$Gy h$^{-1}$ U$^{-1}$. $\Lambda$ is defined as the dose rate at $P(r_0, \theta_0)$ per unit $S_K$.

$\Lambda_{\text{neD,Pq,S}}$ Notation identifying the dose-rate measurements or calculations used to determine $\hat{D}(r_0, \theta_0)$ and the calibration standard to which this dose rate is normalized. For example, $\Lambda_{\text{neD,Pq,S}}$ indicates a dose-rate constant determined from dosimetry measurements made in 1997 and having an $S_K$ traceable to the 1999 NIST standard.

$\text{CON}$ Notation indicating that the reported value of $\Lambda$ is the consensus value determined by the AAPM from published data, with units of cGy h$^{-1}$ U$^{-1}$.

$\text{EXP}$ Notation indicating that the reported value of $\Lambda$ was determined by experimental measurement.

$\text{MC}$ Notation indicating that the reported value of $\Lambda$ was determined using Monte Carlo calculations.

$L$ Active length of the source (length of the radioactive portion of the source) with units of cm.

$L_{\text{eff}}$ Effective active length of the source, with units cm.

LIBD Low-energy Interstitial Brachytherapy Dosimetry subcommittee of the AAPM Radiation Therapy Committee

NIST National Institute of Standards and Technology

$P(r, \theta)$ Point-of-interest, positioned at distance $r$ and angle $\theta$ from the geometric center of the radionuclide distribution.

$\phi_{\text{an}}(r)$ The one-dimensional anisotropy function. At any radial distance $r$, $\phi_{\text{an}}(r)$ is the ratio of dose rate averaged over $4 \pi$ steradian integrated solid-angle to the dose rate at the same distance $r$ on the transverse plane. Dimensionless units.

RTP Radiotherapy planning system. In the context of this protocol, a treatment planning system that can perform dose calculations for brachytherapy implants.

$\text{RTP}$ The distance from the source center to $P(r, \theta)$, with units of cm.

$r_0$ The reference distance, which is 1 cm for this protocol.
The air-kerma strength per history estimated using Monte Carlo methods.

$s_K$

Air-kerma strength: the product of the air-kerma rate $K_{d}(d)$ and the square of the distance $d$ to the point of specification from the center of the source in its transverse plane. $s_K$ is expressed in units of $\mu$Gy m$^2$ h$^{-1}$, a unit also identified by $U$.

The 1985 NIST FAC air-kerma standard.

$s_{K,N85}$

The 1999 NIST WAFAC air-kerma standard.

$\theta$

The polar angle between the longitudinal axis of the source and the ray from the active source center to the calculation point, $P(r, \theta)$.

The reference polar angle, which is 90° or $\pi/2$ radians.

TLD

Thermoluminescent dosimeter, generally composed of LiF.

$U$

The unit of air-kerma strength, equivalent to $\mu$Gy m$^{-2}$ h$^{-1}$ or cGy cm$^{-2}$ h$^{-1}$.

WAFAC

The wide-angle free-air chamber presently used at NIST to determine the air-kerma strength of a low-energy photon-emitting brachytherapy source.

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APPENDIX A: MODEL-SPECIFIC SOURCE DOSIMETRY DATA

The following sections summarize the dosimetry parameters for each source. A description of the source and its references are first provided. Afterwards each dosimetry parameter is discussed briefly.

1. Amersham Health model 6702 and 6711 $^{125}$I sources

The model 6702 source consists of a welded titanium capsule containing $^{125}$I adsorbed on anion exchange resin spheres [Fig. 2(a)]. Although the 6702 source is no longer manufactured, consensus data are included in this compila-
the Loftus standard. Corrections for the new standard were made as were corrections for the Solid Water™ phantom to liquid water. The 6711 average $\mu_{\text{exp}} = 0.980 \text{cGy h}^{-1} \text{U}^{-1}$ and $\mu_{\text{MC}} = 0.950 \text{cGy h}^{-1} \text{U}^{-1}$ agree within 3%. The Monte Carlo values agree to within 3%. The Monte Carlo values agree to within 3%. The Monte Carlo values agree to within 3%. The Monte Carlo values agree to within 3%. 37,110 The Monte Carlo values agree to within 3%. The Monte Carlo values agree to within 3%. The Monte Carlo values agree to within 3%. The Monte Carlo values agree to within 3%. The Monte Carlo values agree to within 3%.
The average of the Monte Carlo values from the dataset of Williamson and Hedtjarn is $1.0165 \text{cGy h}^{-1} \text{U}^{-1}$. Therefore the average of these values, $\mu_{\text{CON}}$, is that presented in Table I.

1.2. 6702 and 6711 $g(r)$

For the model 6702 and the 6711 sources, the measured and Monte Carlo values for $r > 1$ cm agree within the experimental uncertainties. The agreement is within 5% for the 6702 source and within 7% for the 6711 source. Table II shows $\mu_{\text{CON}}(r)$ for both models (6702 and 6711), and for line- and point-source approximations. The references for the consensus datasets are provided.

For the 6702 source, measured results and Monte Carlo calculations for $r \geq 1$ cm agree to within 5% for $1 < r < 4$ cm and within 10% for distances greater than 4 cm. The Monte Carlo results of Hedtjarn et al., Williamson, and Mainegra et al. agree well with one another within the combined uncertainties. Monte Carlo results of Hedtjarn et al. are used since they are the most complete and are most consistent with other data for the model 6702 source.

Published data for the 6711 source indicate agreement between the experimentally measured values and the Monte Carlo calculations for distances greater than or equal to 1.0 cm. Experimental results agree to within 7% for $1 < r < 8$ cm. Monte Carlo results of Williamson and Mainegra et al. agree to within 3%. The Monte Carlo values agree with experimental values to within 5%. Therefore, for 6711 $g(r)$, values from Williamson are used since the calculations cover a wider range, including $r < 1$ cm.

1.3. 6702 and 6711 $F(r, \theta)$

Experimental and Monte Carlo results agree within 5% at larger angles for both source models. Tables IV and V present the model 6702 and 6711 $F(r, \theta)$ data, respectively. The measured anisotropy functions $F(r, \theta)$ for the 6702 source from Nath et al., Furhang and Anderson, Schell et al., and Chiu-Tsao et al. were compared with the Monte Carlo calculations of Weaver and Capote et al. In place of a realistic source geometry model used by other Monte Carlo investigators, Weaver used a simple line-source model for $F(r, \theta)$, in conjunction with a photon fluence anisotropy function measured in air at 100 cm for randomly selecting primary photon trajectories. Other than Furhang and Anderson, all datasets agree fairly well. The 2D anisotropy functions determined by Nath et al. and Capote et al. appear quite “noisy” and were therefore excluded from further analysis. The best remaining dataset is by Weaver. These data are the most uniform and complete, and are recommended as $\mu_{\text{CON}}(r, \theta)$ in (Table IV).

The anisotropy functions $F(r, \theta)$ for the 6711 source from Sloboda and Menon, Furhang and Anderson, and Chiu-Tsao et al., were compared with Monte Carlo calculations by Weaver. Other than Sloboda and Menon, and Furhang and Anderson, there is good agreement. The $1 < r < 5$ cm results for all angles are within 10%, with the exception of $F(1,0^\circ)$. The most uniform and complete dataset seems to be Weaver, and therefore results by Weaver are recommended as the $\mu_{\text{CON}}(r, \theta)$ in Table V for the model 6711 source.

2. Best medical model 2301 $^{125}$I source

In 1992, a double walled encapsulated source of radioactive $^{125}$I on a tungsten substrate was developed for interstitial brachytherapy (Best Medical International, Springfield, VA, model 2300) as described by Rustgi. A sketch of this source is shown in Fig. 2(c). The double walled encapsulation design was intended to provide thinner walls at the ends of the source so that the corresponding angular distributions are more isotropic. In contrast to the model 6711 source, which uses a silver substrate that also serves as the radiographic x-ray marker for source localization in the patient, the model 2300 uses a tungsten rod. $^{125}$I is distributed within a low atomic number cylindrical annulus that surrounds the rod (much like the Bebig source). Because the tungsten $K$-shell binding energy exceeds the maximum energy emitted during $^{125}$I decay, no characteristic $K$-shell x-rays are produced whereas $L$-shell x-rays are readily absorbed in the encapsulation.

In 1993, Nath and Melillo reported the dosimetric characteristics of the model 2300 source. Six years later in 1999, the manufacturer introduced a commercial product based on the earlier design, which has been designated as the model 2301 source. The model 2301 source has a physical length of 4.95 mm and outer diameter of 0.8 mm. The $^{125}$I radionuclide was infused within the organic matrix that was coated on a tungsten rod with an active length of 3.95 mm and a diameter of 0.25 mm [Fig. 2(c)]. Also in 1999, NIST established a WAFAC calibration standard for the air-kerma strength of the model 2301 source.

Meigooni et al. measured the TG-43 dosimetric parameters for the model 2301 source and reported the values based upon the original WAFAC 1999 standard. Because of the 1999 NIST WAFAC anomaly, which was discovered after the publication of Meigooni et al., the air-kerma strength was revised, the value determined as in Table I, and the TG-43 dosimetry parameters reported by Meigooni et al. were corrected to this new value. In 2002, Nath and Yue published independent determinations of TG-43 parameters of the model 2301 source based on TLD measurements.

Finally, Sowards and Meigooni published a TG-43 dosimetry dataset obtained using Monte Carlo methods in both liquid water and Solid Water™.
2.1. 2301 $\Lambda$

For comparison purposes, Sowards and Meigooni published a dose rate constant value of $0.98 \pm 0.03 \text{ cGy h}^{-1} \text{U}^{-1}$ in Solid Water™, and obtained $MC\Lambda = 1.01 \pm 0.03 \text{ cGy h}^{-1} \text{U}^{-1}$ in liquid water.\textsuperscript{117}

In a Solid Water™ phantom, Nath and Yue used LiF TLD detectors which were calibrated against a 6 MV x-ray beam.\textsuperscript{116} A relative energy-response correction factor of 1.41 was used.\textsuperscript{85} Nath’s published $\Lambda$ value was increased by 4.3%, based on $^{125}$I Monte Carlo simulations, to correct for non-water equivalence of the Solid Water™ measurement medium, yielding $\Lambda = 1.02 \pm 0.07 \text{ cGy h}^{-1} \text{U}^{-1}$. Meigooni \textit{et al.} have also measured $\exp\Lambda$ using LiF TLDs in a Solid Water™ phantom using a 6 MV x-ray beam for calibration and a relative energy response correction factor of 1.40. The authors applied 1.05 as the correction factor to account for the Solid Water™ measurement medium. After applying the 1999 WAFAC anomaly correction to the published value, a value of $\Lambda = 1.01 \pm 0.08 \text{ cGy h}^{-1} \text{U}^{-1}$ was obtained based on the authors’ uncertainty analysis.\textsuperscript{115} A further correction was reported in a private communication that resulted in a final value of $\Lambda = 1.03 \text{ cGy h}^{-1} \text{U}^{-1}$ for the Meigooni group,\textsuperscript{86} as described in detail within the publication by Nath and Yue.\textsuperscript{116}

In this protocol, the final measured values of the candidate datasets of Nath and Yue and of Meigooni \textit{et al.} were averaged to obtain a mean value of $\exp\Lambda = 1.025 \text{ cGy h}^{-1} \text{U}^{-1}$. This mean measured value was averaged with $MC\Lambda = 1.01 \text{ cGy h}^{-1} \text{U}^{-1}$ yielding $CON\Lambda = 1.018 \text{ cGy h}^{-1} \text{U}^{-1}$.

2.2. 2301 $g(r)$

The measured radial dose function of Meigooni \textit{et al.}\textsuperscript{115} for the Best model 2301 source is slightly more penetrating than that of model 6711 $^{125}$I source, and slightly less penetrating than that of the model 6702 $^{125}$I source at distances beyond 2 cm. Monte Carlo results from Sowards and Meigooni were chosen as the $CONg(r)$; these values are presented in Table II.

2.3. 2301 $F(r, \theta)$

The anisotropy function of the Best $^{125}$I source (model 2301) was measured at 2, 4, and 6 cm, and at different $\theta$ angles by Nath and Yue and at 2, 5, and 7 cm by Meigooni \textit{et al.} Monte Carlo calculations at distances of 1, 2, 3, 4, 5, 6, and 7 cm were reported by Sowards and Meigooni. A comparison of the measured and calculated values indicates good agreement between the different datasets. Following the consensus procedure, $CONF(r)$ was chosen based on results reported by Sowards and Meigooni with the exception of 6 cm data which exhibited larger statistical noise. Therefore, results from Sowards and Meigooni were used for $CONF(r, \theta)$, and are presented in Table VI.

3. North American Scientific Inc. model MED3631-A/M $^{125}$I source

The North American Scientific Inc. (NASI) model MED3631-A/M source\textsuperscript{45,48,118,119} was introduced to the market in October 1998 following a brief appearance by the model MED3631-A/S source.\textsuperscript{120,122} The capsule is made of titanium, with a 0.81 mm outer diameter and 0.05 mm wall thickness, and a nominal length of 4.5 mm with spherical end welds of thickness 0.05 to 0.15 mm. Inside the MED3631-A/M are four polystyrene ion exchange resin beads, within which $^{125}$I is uniformly distributed. The four beads are separated into two sets by two gold-copper radio-opaque markers. Both the beads and markers have a nominal diameter of 0.5 mm, and are free to move about within the capsule interior [Fig. 2(d)].

The only complete (2D) experimental characterization of brachytherapy dosimetry parameters was performed by Wallace and Fan.\textsuperscript{120} They irradiated TLD-100 rods in tissue- and water-equivalent plastic phantoms. Detectors were calibrated using a $^{60}$Co teletherapy beam with tissue-equivalent phantom corrections, $C_p(r)$, of $C_p(r=0.5 \text{ cm}) = 0.778$ and $C_p(r=7 \text{ cm}) = 1.053$. Measurements were performed in 1998, so corrections for the 1999 WAFAC anomaly were not necessary since the 2000 NIST WAFAC measurements differed by <1% compared to the 1998 calibration. Table I shows the value used now based on a 2001 calibration. Because the $G(r, \theta)$ used by all investigators was based on a four point source model, all $g(r)$ and $F(r, \theta)$ datasets were converted using an active length of 4.2 mm to adhere to the 2D formalism of this protocol.

Rivard published a complete, 2D TG-43 dosimetry dataset for the MED3631-A/M source using Monte Carlo methods developed from previous studies.\textsuperscript{123–126} The effect of internal component motion on dose distributions external to the capsule was considered for the first time. The WAFAC was not simulated, and a 30 cm diameter liquid water spherical phantom encompassed the source. Radii ranged from 0.25 to 10 cm, and the angular range was 0° to 180° with 1° increments. Air-kerma strength was determined in a 6 meter diameter sphere of dry air by multiplying the total air-kerma strength, integrated over all photon energies, by 1.049 to account for photon transmission in air at 1 meter, and by 0.897 to account for Ti $K$-shell x rays. A corrected value was later published, recognizing that the $S_{K,x94}/S_{K,N85}$ factor measured by NIST does not accurately model the influence of Ti x rays in the geometry used for Monte Carlo calculations.\textsuperscript{127} Statistical uncertainties ranged from 0.1% to 2% for $F(r, \theta)$ on the transverse plane to the source ends, respectively. Statistical uncertainties in $g(r)$ and $\Lambda$ were typically ±1%, and ±3%, respectively.

3.1. MED3631-A/M $\Lambda$

Wallace and Fan reported $\Lambda = 1.056 \text{ cGy h}^{-1} \text{U}^{-1}$, and Li \textit{et al.} reported $\Lambda = 1.067 \text{ cGy h}^{-1} \text{U}^{-1}$. This average yields $\exp\Lambda = 1.0615 \text{ cGy h}^{-1} \text{U}^{-1}$. Rivard calculated $\Lambda = 1.066 \text{ cGy h}^{-1} \text{U}^{-1}$, but this value was later corrected to $1.011 \text{ cGy h}^{-1} \text{U}^{-1}$ based on an inappropriate correction methodology.\textsuperscript{127} Taking an equally weighted average of 1.0615 and 1.011, Table I shows $CON\Lambda = 1.036 \text{ cGy h}^{-1} \text{U}^{-1}$.

Li \textit{et al.} performed measurements only on the transverse-plane in 1999.\textsuperscript{48} Dosimetry measurements were made using
TLD-100 chips and a diode in a large water phantom. Irradiation in the water phantom was accomplished by tapping the TLD chips onto the tip of the diode detector for 30 minutes. No phantom material correction was employed, but the TLD energy response function of Weaver et al. was used. Calculation of \( P \) was based on the ratio of measured readings of MED3631-A/M and 6702 \(^{125}\)I sources and using the 6702 calculation of Let al. readily resolvable. Therefore, the measured data of Li Rivard and by Li cm. Consequently, the difference between results obtained by Wallawse and Fan (\( r \)) shows consistent behavior than that of Wallace and Fan. Agreement among converted \( F(r, \theta) \) results from both sets of investigators was good, with \( F(r, \theta \sim \theta^2) \sim 0.72 \pm 0.05 \) for 0.25 < \( r \) < 10 cm. Furthermore, agreement among \( \phi_{\text{abs}}(r) \) results reported by Rivard and by Wallace and Fan was similarly good (\( \pm 3\% \)).

### 4. Bebig/Theragenics Corporation model I25.S06 \(^{125}\)I source

The Bebig/Theragenics Corporation model I25.S06 \(^{125}\)I source (IsoSeed) was introduced to the market in July 1999 initially under the name Symmetra. On February 4, 2003, Theragenics Corporation purchased the U.S. \(^{125}\)I prostate brachytherapy business of BEBIG Isotopen und Medizintechnik GmbH—including the manufacturing and distribution rights to the IsoSeed\(^ {125}\)I brachytherapy source distributed by Isotope Products Laboratories. Theragenics Corporation distributes this source under the brand name I-Seed. The source design for both IsoSeed\(^ {125}\)I and I-Seed are the same, and the model (I25.S06) also remains the same. Its encapsulation consists of a 0.05 mm thick titanium capsule with spherical end-welds (0.44–0.48 mm thick) similar to those of the 6711 source family. The radioactive core consists of a 3.5 mm long cylindrical ceramic (alumina, 2.88 g/cm\(^3\)) annulus within which the radioactive iodine \(^{125}\)I is uniformly distributed. A gold marker, 0.17 mm diameter and 3.5 mm long placed inside the ceramic core, permits radiographic source localization. A schematic diagram is shown in Fig. 2(e).

Hedtjarn \( \text{et al.} \)\(^ {42}\) describes a complete Monte Carlo study based mainly on the DLC-99 cross-section library. The estimator used was a bounded next-flight point-karma estimator. Patel \( \text{et al.} \) described TLD measurements of \( \Lambda, g(r), \) and \( F(r, \theta) \) for a limited number of distances (1–5 cm).\(^ {57}\) This group subjected the widely used Solid Water\( ^{\text{TM}} \) material to chemical analysis and found its calcium content, which compensates for nonwater equivalence of the organic polymer composition of the basic material, to differ significantly from the vendor’s specified atomic composition. Based on the measured composition, Williamson’s PTRAN code was used to calculate distance and TLD-size dependent energy response correction factors (1.3–1.5). The measurement distance range was 1–4 cm. Finally, Williamson\(^ {44}\) compared \( \text{MC}\Lambda \) with and without full simulation of the WAFAC geometry, using the DLC-146 cross-section library, and found that the WAFAC and point-karma detectors agreed within 1%.\(^ {44}\) In this case, the bounded next flight estimator for water kerma was used, except for distances less than 3 mm, where the once-more-collided point flux estimator was used. The expected-value track-length estimator was used for the WAFAC simulation. These two references, Hedtjarn \( \text{et al.} \) and Williamson,\(^ {42,44}\) constitute the only published Monte Carlo data available for this source model.

### 4.1. I25.S06 \( \Lambda \)

Using Monte Carlo methods, Hedtjarn \( \text{et al.} \) estimated \( \Lambda \) using the DLC-146 cross-section library and by modeling the WAFAC geometry. Their \( \text{MC}\Lambda \) value, 0.991 cGy h\(^{-1}\) U\(^{-1}\), was averaged with the \( \text{EXP}\Lambda \) value, 1.033 cGy h\(^{-1}\) U\(^{-1}\), by
Patel et al. The two values agree within the experimental uncertainties, and the \( \text{CON}_{\text{A}} \) value is given in Table I.

4.2. IS-12501 \( g(r) \)

The \( g(r) \) data calculated by Hedtjarn et al. and measured by Patel et al. are based upon a line source with \( L = 0.35 \) cm. These two datasets agree within experimental uncertainties (5%) except for \( g(0.5) \). Due to its larger coverage of radial distance and closer coverage towards the source, the Monte Carlo \( g(r) \) data of Hedtjarn et al. are recommended.

4.3. IS-12506 \( F(r, \theta) \)

Measured anisotropy functions by Patel et al., based on an active length of 0.35 cm, were compared to Monte Carlo data by Hedtjarn et al. and Williamson. For completeness, the anisotropy function derived from the 4 cm Monte Carlo calculations, which was omitted from the published paper, was added. Agreement within 5% was usually observed. The discrepancies were random and not indicative of different trends between the measured and computational approaches. The Hedtjarn et al. data are recommended and given in Table VIII.

5. Imagyn Medical Technologies Inc. isostar model IS-12501 \(^{125}\)I source

International Isotopes Inc. (Denton, TX, now a division of Imagyn Medical Technologies Inc.), produced this source. It is marketed by Imagyn Medical Technologies, Inc. under the trade name “isostar IS-12501.” This source model first became available for analysis in 1999, and was introduced to clinical sites later that year. The design consists of five 0.56 mm diameter silver spheres on which \(^{125}\)I silver iodide is encapsulated [Fig. 2(f)]. The silver spheres are encapsulated in a titanium tube whose ends are laser welded.

There are four pertinent references for this source. Complete experimental and Monte Carlo results are given in Gearheart et al. and experimental results by Nath and Yue, respectively. Experimental measurements (TLD in Solid Water\(^{TM} \)) of \( \Lambda, g(r) \) from 0.5 cm to 10 cm, and anisotropy function at 2 cm and 5 cm were first reported by Gearheart et al. This work also contains Monte Carlo calculations of \( g(r) \) and \( F(r, \theta) \), both in water and in Solid Water\(^{TM} \) with ratios between each media. These ratios were used to convert the TLD measurements of \( \Lambda \) in Solid Water\(^{TM} \) to that in liquid water. The PTRAN Monte Carlo code was used, with the HUGO DLC-99 cross-section libraries. The bounded next-flight point-kerna estimator was used. Nath and Yue presented TLD measurements of \( \Lambda \) and \( g(r) \) from 0.5 cm to 6 cm. Monte Carlo calculations were used to relate \( \Lambda \) in water to the measurements in Solid Water\(^{TM} \).\(^{57} \)

5.1. IS-12501 \( \Lambda \)

Ibbott and Nath explained that when the \( \Lambda \) value of Gearheart et al. is corrected using the revised 1999 NIST calibration agreement with Nath and Yue improved to 3%. Ibbott and Nath published \( \text{CON}_{\text{A}} = 0.940 \text{ cGy h}^{-1} \text{U}^{-1} \), based upon the methodology in this protocol, and this value is given in Table I.

5.2. IS-12501 \( g(r) \)

Gearheart et al. and Nath and Yee measured \( g(r) \) in Solid Water\(^{TM} \). In both cases, \( g(r) \) was calculated using the line-source approximation method. Gearheart et al. also published Monte Carlo calculation of \( g(r) \) in liquid water. Analysis revealed the TLD measurements agreed with the Monte Carlo calculations within \( -8\% \) to \( +6\% \) with 1 standard deviation of \( +4\% \) (1\sigma). Consequently, Gearheart et al. Monte Carlo values in water are recommended as \( \text{CON}_{\text{A}} g(r) \), and are listed in Table II.

5.3. IS-12501 \( F(r, \theta) \)

Nath and Yee did not measure \( F(r, \theta) \). Gearheart et al. published TLD measurements in Solid Water\(^{TM} \) and also performed Monte Carlo calculations in both Solid Water\(^{TM} \) and liquid water. The geometry function was modeled as a line source with active length of 0.34 cm. Monte Carlo calculations were performed at 1, 2, 3, 5, and 7 cm to facilitate calculation of \( \phi_{\text{an}}(r) \) at these distances. Comparison of measured and calculated data demonstrate good agreement within combined uncertainties of 10%. Consensus \( F(r, \theta) \) and \( \phi_{\text{an}}(r) \) data from Gearheart et al. are presented in Table IX.

6. Theragenics Corporation model 200 \(^{103}\)Pd source

The model 200 (TheraSeed\(^{TM} \)) source was introduced by Theragenics Corporation in 1987, and remained the sole commercially available interstitial \(^{103}\)Pd source until 1999. The encapsulation is a 0.056 mm thick Ti tube with a measured external length of 4.50 mm and average measured outer diameter of 0.83 mm, respectively. The tube ends are closed by means of inverted “end-cups” composed of 0.040 mm thick Ti metal welded to the Ti tube. Using transmission radiography and microscopic examination, Monroe and Williamson showed that the end-cup shape is not well approximated by the right cylindrical shape used in early, simplified Theragenics Corporation manufacturing illustrations.\(^{40} \) The internal source components include two graphite pellets, modeled as right circular cylinders with 0.56 mm diameters and 0.89 mm long, upon which a mixture of radioactive and nonradioactive palladium is added. The graphite pellets are separated by a cylindrical lead marker. Dosimetric analysis is complicated by the fact that two manufacturing techniques were used to produce the \(^{103}\)Pd used in these sources: lower specific activity reactor-produced \(^{103}\)Pd until 1995 and higher specific activity accelerator-produced palladium used thereafter. The older reactor-produced heavy seeds had thicker layers of palladium metal plated on the graphite pellets, ranging from 8 \( \mu \)m to 23 \( \mu \)m (200–570 \( \mu \)g/pellet).\(^{7} \) The Monte Carlo study by Monroe and Williamson assumed a 10.5 \( \mu \)m thick (260 \( \mu \)g/pellet) layer.\(^{40} \) Monroe and Williamson also modeled the current light seed configuration with a pellet coating of 2.2 \( \mu \)m for \(^{103}\)Pd per pellet.\(^{109} \) While pellet coating thickness has been shown to minimally influence the source dosimetric characteristics, most of the published dosimetry studies,
including the original TG-43 protocol dataset for the model 200 source, are based upon the obsolete heavy seed geometry.\textsuperscript{7,6,10,6,107}

Until 1999, there was no air-kerma strength standard for the model 200 source. Theragenics Corporation maintained an “apparent activity” standard based upon intercomparison of photon fluence rates from model 200 \textsuperscript{103}Pd sources and \textsuperscript{109}Cd activity standards using a NaI(Tl) detector. A detailed history of these practices is given in LIBD’s recommendations on \textsuperscript{103}Pd calibration and dose-prescription practices.\textsuperscript{7} Briefly, the \( \Lambda \) value published in the original TG-43 protocol was based upon the Theragenics Corporation \( A_{\text{app},TSS} \) standard which was initiated in 1988. TLD measurements of \( \Lambda \) by Meigooni and Chiu-Tsao were normalized to the Standard which was initiated in 1988. TLD measurements of \( \Lambda \) by Meigooni and Chiu-Tsao were normalized to the Standard which was initiated in 1988. TLD measurements of \( \Lambda \) by Meigooni and Chiu-Tsao were normalized to the Standard which was initiated in 1988. TLD measurements of \( \Lambda \) by Meigooni and Chiu-Tsao were normalized to the Standard which was initiated in 1988. TLD measurements of \( \Lambda \) by Meigooni and Chiu-Tsao were normalized to the Standard which was initiated in 1988. TLD measurements of \( \Lambda \) by Meigooni and Chiu-Tsao were normalized to the Standard which was initiated in 1988. TLD measurements of \( \Lambda \) by Meigooni and Chiu-Tsao were normalized to the Standard.\textsuperscript{130} In 1999, the vendor’s \( A_{\text{app},TSS} \) calibration was intercompared with the new 1999 NIST WAFAC standard, and the 1999 NIST standard replaced the vendor’s calibration in March 2000. These initial NIST WAFAC calibrations were affected by the 1999 WAFAC anomaly. On average, WAFAC calibrations made after March 2000 were 5.3\% less than calibrations performed during 1999. On March 5, 2001, Theragenics Corporation adopted (re: letter to users dated Feb 14, 2001) the corrected NIST calibrations.

Six published papers were reviewed to determine the full consensus dataset for the model 200 light seed.\textsuperscript{40,6,60,131–133} Monroe and Williamson present comprehensive Monte Carlo-based dosimetry data for both reactor- (heavy) and cyclotron- (light) produced sources.\textsuperscript{40} Their results indicate that the heavy and light seed \( g(r) \) are nearly identical. Nath \textit{et al.}\textsuperscript{131} has published a measured \( \Lambda \) for the light seed while Yue and Nath published measured light seed anisotropy functions.\textsuperscript{135} Chiu-Tsao and Anderson, and Meigooni \textit{et al.} present measured \( g(r) \) for the heavy seed design.\textsuperscript{40,132} Results by Williamson and Monroe were based upon the PTRAN Monte Carlo code version 7.43 and used the DLC-146 cross-section library and included a complete geometric model of the WAFAC. A bounded next flight point kerma estimator was used. This estimator resulted in a 1\( \sigma \) uncertainty between 0.2\% (near the source) to 2.5\% (far from the source).

\subsection*{6.1. 200 \( \Lambda \)}

For \textit{CON}\( \Lambda \), Nath’s measured value (corrected by 1.05 to reflect the 1999 WAFAC measurement anomaly) was averaged with Monroe and Williamson’s Monte Carlo estimate, yielding the value given in Table I. These two values agreed within 2\%. Also, note that the Model 200 source \( \Lambda \) is nearly independent of the thickness of the Pd metal matrix.\textsuperscript{46}

\subsection*{6.2. 200 \( g(r) \)}

The \( g(r) \) results measured by Chiu-Tsao and Anderson using TLDs were recalculated using a line-source approximation geometry function with \( L = 0.423 \) cm. The graphical comparison indicates that the MC data agree better with each measured dataset than the two measurements agree with one another. Except for the 0.1 cm measurement point, very good agreement with measured results by Chiu-Tsao and Anderson at short distances is achieved. The light seed \( g(r) \) Monte Carlo data of Monroe and Williamson are recommended as consensus data (Table III) since they include data from 0.1 cm to 12.5 cm. Williamson demonstrates using Monte Carlo simulations that geometric differences between the light and heavy seeds do not significantly influence the radial dose function.\textsuperscript{46}

\subsection*{6.3. 200 \( F(r,\theta) \)}

After conversion to a common active length of 0.423 cm, the Yue and Nath \( F(r,\theta) \) measured data were compared to the Monroe and Williamson Monte Carlo data. Excellent agreement of \( F(r,\theta) \) between Monte Carlo results of Monroe and Williamson and measured results by Yue and Nath is observed, often within 5\%. Since the Monroe and Williamson light seed data cover the distance range from 0.25 cm to 7.5 cm and were similar to the heavy seed data, they are recommended as the consensus dataset (Table X).

\section*{7. North American Scientific Inc. model MED3633 \textsuperscript{103}Pd source}

The model MED3633 source was introduced to the market in February 1999, and is currently distributed by the manufacturer, NASI. It has the same internal/external geometry as the MED3631-A/M [Fig. 2(d)] with \( L = 4.2 \) mm. However, \textsuperscript{103}Pd is distributed only on the surface of the ion exchange beads. During this time, the NIST 1999 WAFAC measurement anomaly impacted measurements of \( \Lambda \) by +3.2\%. A letter to end-users was sent out in late 2000 discussing the calibration change, and shift in \( \Lambda \). There are only three peer-reviewed papers which assess the MED3633 2D dosimetry parameters.

Wallace and Fan measured 2D brachytherapy dosimetry parameters in a water-equivalent phantom using TLD rods and an annealing procedure identical to that previously described for the MED3631-A/M source.\textsuperscript{134} A phantom correction factor of 1.0235 obtained by Luxton and Wallace was used to calculate \( \Lambda \),\textsuperscript{135,136} and a TLD energy response correction of 1.41 obtained by Meigooni \textit{et al.} was also used.\textsuperscript{132} Radii on the transverse plane are listed to range from 0.17 to 7 cm, yet Table II of this paper contains an entry for \( r = 0.15 \) cm. Due to the small detector size (1 mm diameter \( \times \) 6 mm long LiF TLD-100 rods), measurements at distances \( \geq 0.5 \) cm may be considered free of volume-averaging artifacts.

Li \textit{et al.} measured \( g(r) \) and determined \( \Lambda \) for the MED3633 source in a large water phantom using a computer-controlled diode-electrometer system.\textsuperscript{137} Li \textit{et al.} used Williamson’s PTRAN Monte Carlo photon transport code with the DLC-99 cross-section library, but did not describe the \textsuperscript{103}Pd photon energy spectrum, material densities and compositions, or the calculation geometry. The number of particle histories was such that 1\( \sigma \) standard uncertainty about the mean was less than 2\%. The authors state the source geometry was explicitly modeled, including the 0.15 mm thick semispherical end welds and 0.1 mm bead-marker

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spacing. No information was given regarding the manner in which $S_w$ was determined. However, the bounded next flight point kerma estimator was employed.

Rivard calculated the 2D dosimetry parameters using MCNP version 4B2 and the DLC-189 cross-section library similar to the MED3631-A/M calculations (accounting for motion of internal source components). Results for $g(r)$ and $F(r, \theta)$ were evaluated over the 0.25 to 10 cm distance range, and $F(r, \theta)$ was evaluated from $0^\circ \leq \theta \leq 180^\circ$ in $1^\circ$ increments (though only $10^\circ$ increment data were reported). The Ti characteristic x-ray contributions were removed offline by binning kerma on energy and removing contributions <5 keV. The energy dependence of TG-43 dosimetry parameters was analyzed by discretizing the polyenergetic $10^3$Pd spectra, and performing comparisons with results presented by Chen and Nath, Luxton and Jozsef, and Carlsson and Ahnjeso. 

7.1. MED3633 $\Lambda$

Wallace and Fan reported a measured $\Lambda$ value of 0.680 $\pm 0.033$ cGy h$^{-1}$ U$^{-1}$, yielding the value of 0.702 $\pm 0.034$ cGy h$^{-1}$ U$^{-1}$ when corrected for the 1999 NIST WAFAC anomaly. Using a diode scanning system, a liquid water phantom, and an in-house cross-calibration technique, Li et al. reported two measured values (0.714 and 0.682 cGy h$^{-1}$ U$^{-1}$) before applying the +3.2% 1999 NIST WAFAC anomaly correction (Table I). Though the corrected average of these two diode readings would yield 0.720 cGy h$^{-1}$ U$^{-1}$, these measurements are not included in this consensus since a cross-calibration method using a source from a different manufacturer is discouraged. Therefore, Wallace and Fan gave $\Lambda = 0.702$ cGy h$^{-1}$ U$^{-1}$ with $\exp \Lambda$ also equal to 0.702 cGy h$^{-1}$ U$^{-1}$. Using MCPT, Li et al. calculated 0.677 cGy h$^{-1}$ U$^{-1}$, and Rivard calculated 0.672 cGy h$^{-1}$ U$^{-1}$ using discretized photon energy fluence estimators. Consequently, $\text{MC} \Lambda = 0.6745$ cGy h$^{-1}$ U$^{-1}$ was obtained. Combining results, $\text{CON} \Lambda = 0.688$ cGy h$^{-1}$ U$^{-1}$ is shown in Table I.

7.2. MED3633 $g(r)$

While the MCNP results of Rivard covered the largest radial distance range and came closest to the source, the MCNP $g(r)$ results could not be recommended. As was the case for the MED3631-A/M source, Rivard used the default MCNP cross-section library which is now known to cause significant differences following radiation penetration through multiple pathlengths due to obsolete photon cross-section data. Thus, the $g(r)$ results of Li et al. generated using MCPT and updated cross-section data are recommended for $\text{CON} \Phi(r)$ data, with Rivard's data recommended (italicized) only for $r < 1$ cm (Table III) where cross-section data selection was less crucial. Note that the Rivard $g(0.5)$ data exactly matched that of Li et al., i.e., $g(0.5) = 1.243$. For $r > 4$ cm the Rivard data differed from the Li et al. data by more than 10%, while Wallace and Fan $g(r)$ data agreed with the Li et al. data (except at $r = 6$ cm where the diode signal was quite low) within ±4%. Compared to the Li et al. MCPT data, the Li et al. diode data varied by ±7% for 0.5 $< r < 1.5$ cm, and are not considered reliable. Therefore the $\text{CON} \Phi(r)$ is a combination of results by Rivard at close distances and Li et al. for $r > 1$ cm.

7.3. MED3633 $F(r, \theta)$

Rivard's MED3633 $F(r, \theta)$ dataset covered the largest angular and radial ranges, and its accuracy was expected not to be influenced by the outdated photon cross-section libraries since data were normalized to a given distance. As for the MED3631-A/M source, the dose rate data above and below the transverse plane were averaged to account for the asymmetric geometric source model, and used to derive the consensus dataset 2D anisotropy function data (Table XI). These averaged data were compared with the Monte Carlo data by Li et al. and the TLD results from Wallace and Fan at common radial distances of 1, 2, and 5 cm. Over these radii, the Li et al. results agreed with Rivard's data within ±7% (typically +4%). While differences as large as 20% were noted for small polar angles, these discrepancies may be attributed to different source models or the averaging technique used for the $F(r, \theta = 0^\circ – 180^\circ)$ data. In comparison to the MCNP results, the $F(r, \theta)$ dataset of Wallace and Fan exhibited unexpected irregularities (+13% at $r = 5$ cm, $\theta = 80^\circ$, and +18% at $r = 1$ cm, $\theta = 40^\circ$).

APPENDIX B: NIST AIR-KERMA STRENGTH STANDARDS FOR LOW-ENERGY PHOTON-EMITTING SOURCES

1. NIST 1985 standard using the free-air chamber

The National Institute of Standards and Technology (NIST) maintains the U.S. primary air-kerma standards for x-rays in the energy range of 10 to 300 keV and for photon-emitting radionuclides such as $^{137}$Cs, $^{192}$Ir, $^{103}$Pd, and $^{125}$I. The primary standard for $^{137}$Cs and $^{192}$Ir sources consists of Bragg–Gray cavity chambers. To provide similar traceability for low-energy photon-emitting $^{125}$I sources, Lofts developed a primary standard for $^{125}$I sources in 1985 based on the Ritz parallel-plate free-air chamber (FAC), the national primary x-ray standard for superficial therapy beams. This chamber was used to measure the exposure rate in free-space on the transverse plane of model 6711 and 6702 sources. Because the Ritz FAC background current was high relative to signal strength expected from a single source, this device was limited to a calibration arrangement of a combination of 4 to 6 sources. These calibrations were then transferred to a spherical aluminum re-entrant ionization chamber which served as the secondary standard for routine calibrations. Uncertainties (2σ = 95% confidence level) for the transferred measurements were 3% and 4% for the model 6702 and 6711 $^{125}$I sources, respectively. Measurement uncertainties for subsequent source calibrations using the re-entrant chamber were estimated to be 5% and 6% for the 6702 and 6711 sources, respectively. This Lofts calibration standard became available in 1985 and has been referred to as the NIST 1985 air-kerma strength standard.
(S_{K,N99}) in recent AAPM guidance protocols. Soon after introduction of this standard, Kubo called attention to the influence on exposure measurements made in air by Ti K-shell characteristic x rays. These low-energy x rays (<5 keV) are clinically insignificant because they are largely absorbed by tissue or water within 1 mm of the source. However, these x rays can affect air-kerma strength measurements. Because of the extreme difficulty in using the Ritz FAC for such measurements, NIST chose not to repeat this standardization process until a new instrument could be developed, precluding the addition of new low-energy source models to the NIST system of standards or periodic inter-comparisons between the Ritz FAC and NIST re-entrant chamber. Monte Carlo calculations by Williamson examined the effects of x rays <5 keV on Loftus’ FAC measurements and data analysis procedures, and found that the air-kerma rate was overestimated because the contributions by these x rays were included in the measurements.

2. NIST 1999 standard using the wide-angle free-air chamber

2.1. The wide-angle free-air chamber

By the early 1990s, NIST was prompted to develop a new standard for brachytherapy sources because of deficiencies in the existing primary standard, the need to develop a new instrument to directly measure air-kerma rate from individual sources (particularly those of low-energy photon-emitters such as ^{103}Pd and ^{125}I), and the need to calibrate sources of newer design. In 1993, Loevinger developed the wide-angle free-air chamber (WAFAC). Measurements were initiated in 1998, and the new NIST WAFAC standard was formally introduced on January 1, 1999. Numerous calibrations based on this standard have been performed for the still-growing number of new source designs. WAFAC results were compared to those of the Ritz FAC for four different NIST low-energy x-ray beam qualities. The average level of agreement was 1.003 ± 0.003.

Figure 3 shows a schematic diagram of the WAFAC chamber. It is a cylindrical chamber with circular symmetry about the beam-axis, and consists of:

(a) a front, circular, aluminized-polyethylene terephthalate (PET) high voltage electrode, held at a potential V;
(b) a back, circular, aluminized-PET electrode that is divided into a central circular area, defining the collecting electrode, and an annular guard ring, both held at ground potential;
(c) a circular aluminum middle electrode separating the front and back electrodes, held at potential V/2 to shape the electric field; and
(d) a mechanical support and auxiliary measurement instrumentation.

An aluminum filter, placed between the source-positioning device and the tungsten-alloy aperture, eliminates the Ti K-shell x rays. Among other correction coefficients, attenuation of the penetrating components of source spectra by the aluminum filter is accounted for. The aperture has a diameter of 8 cm, and is placed at a nominal distance of 30 cm from the source. This allows the measurement of radiation in a cone with a half-angle of about 7.6°, rather than the ~1° cone for the Ritz FAC measurements, resulting in a 40-fold increase in solid angle; hence the “wide-angle” description. The effective or defined volume is ~704 cm³, and the collecting volume is ~2474 cm³. This larger effective volume increases WAFAC sensitivity 100-fold compared to the Ritz FAC. Moreover, the ratio of effective to collecting volumes is about 0.28 for the WAFAC compared to only about 0.01 for the Ritz FAC, giving an improved signal-to-background ratio. While the Ritz FAC was limited to measurements of multiple source arrangements, the WAFAC is able to measure S_K with a precision of 0.01 μGy m⁻² h⁻¹ for individual sources with strengths as low as 1.00 μGy m⁻² h⁻¹.

An automated version of the WAFAC was constructed for computer-controlled, motor-driven, variable-length middle electrode length, while holding fixed the positions of the aperture plane and the center plane of the collecting volume to remove detector measurement artifacts. Results from both WAFACs have been compared for a large number of sources of various designs, showing agreement to within 0.5%. Determinations of air-kerma strength (S_K) using the WAFAC are referred to as S_{K,N99} in recent AAPM guidance documents, where N indicates the measurement was performed at NIST and 99 indicates use of the January 1, 1999 WAFAC standard. WAFAC S_{K,N99} determinations have 1.4% Type-B (systematic) uncertainties, and total uncertainties of typically 2% when including Type-A (statistical) uncertainties which depend on source strength.

2.2. Impact of volume averaging by the NIST WAFAC

Because of its large aperture, the WAFAC averages photon fluence over a 7.6° half-angle cone centered about the source transverse plane. Using Monte Carlo simulation techniques, Williamson et al. have shown that WAFAC calibrations can deviate significantly from those based upon point detector air-kerma strength measurements for certain types of source geometries. Such source geometries contain internal components with sharp corners, e.g., right circular cylinders, and are coated with radioactive, radiopaque materials. In the Theragenics Corporation model 200 source (cf. Appendix A.6. for more detail), photons emitted by the Pd-metal coatings on the planar end surfaces traverse moderate thicknesses of Pd metal and contribute to the dose rate in condensed medium at short distances, but are much more heavily self-absorbed at typical calibration distances and therefore, do not contribute significantly to transverse-plane air-kerma rate measurements. This can result in photon-fluence anisotropy factors as large as 1.25 over the solid angle of which the WAFAC integrates.

While there is little direct experimental confirmation of such distance- and angle-dependent radiation self-absorption effects and anisotropy near the transverse plane, the indirect
evidence is persuasive. In the case of the model 200 source, normalizing to point air-kerma strength calculations lead to dose-rate constant values that are sensitive to small changes in internal source geometry and differ from experimental measurements by as much as 17%. Similar but smaller effects of ~5% occur for the models 6711 and STM1251 sources. In contrast, Monte Carlo simulations incorporating the WAFAC measurement geometry reveal no such sensitivity, and result in dose-rate constant (Sec. III.A2) values having close agreement with experimental measurements. Furthermore, significant anisotropy implies that any air-kerma rate measurements based upon a point detector will have large uncertainties due to sensitivity to source alignment and deviation of the actual source geometry from its idealized specifications. Despite its metrological impurity, the current WAFAC standard serves the clinical community well and has many advantages over previous standards. By averaging air-kerma strength over regions of significant and possibly poorly reproducible anisotropy near the source transverse-plane, dosimetric uncertainties caused by misalignment and source geometry specification uncertainties are substantially mitigated.

During the development and testing of the WAFAC in 1997–1998, extensive intercomparisons were made between the WAFAC and the NIST re-entrant chamber (the Loftus transfer standard) for Models 6702 and 6711 sources. The results from 10 sources established a ratio of the new NIST WAFAC standard \((S_{K,999})\) to the old Loftus standard \((S_{K,999})\) of 0.898±0.014 for 6702 sources and 0.896±0.010 for 6711 sources, and 0.897±0.011, combining the two models. Based on this average, the AAPM recommended using \((S_{K,999})/(S_{K,999}) = 0.897\) to convert between the two standards for all applicable 125I source models (Amersham 6711 and 6702 and NASI models 3631 A/S and A/M). Because they were so tedious, NIST discontinued periodic intercomparisons of Loftus re-entrant chamber and WAFAC measurements in 1999. In preparation for the introduction of the new 125I standard, 6702 and 6711 sources were measured with the WAFAC and circulated to the AAPM-Accredited Dosimetry Calibration Laboratories (ADCLs), enabling them to establish their secondary standards. Later, similar sources were circulated in Spring 1999 among the ADCLs in a successful proficiency test (NIST was not involved). The new NIST standard based on the WAFAC was formally introduced on January 1, 1999. At that time, NIST also began the routine measurements of the new 103Pd and 125I source models as well as the 6702 and 6711 sources. Constancy checking of the WAFAC was performed by taking readings with each source type using two commercial well-illumination chambers: a Standard Imaging HDR 1000 Plus, and a Capintec CRC-127R. During 1999 a new automated WAFAC was tested, and agreement with the original WAFAC was repeatedly found to be at the 0.1–0.2% level; the use of the new WAFAC was phased in. In December of 1999, exceptionally large leakage and background currents were noted. The new WAFAC was disassembled, cleaned, reassembled, and compared with the original WAFAC—again with agreement to within 0.1–0.2%.

2.3. 1999 WAFAC measurement anomaly

In January 2000, NIST noticed a shift in well-chamber calibration coefficients for a batch of Bebig 125I sources and a batch of IBt 103Pd sources. By February, shifts were found also for the 6702 and for the 6711 models, and well-chamber measurements by the ADCLs and manufacturers indicated similar shifts of 0–7% between the 1999 and 2000 WAFAC calibrations (as well as those done in 1998). However, the new and original WAFACs were still in agreement. NIST intensified its investigation of this anomaly, completely checking all systems, mechanical, electrical, environmental, software, etc., particularly any factor that could equally affect both WAFAC instruments. More calibrations in 2000 confirmed the situation: an apparent downward shift in the WAFAC air-kerma strength of approximately 3% for 125I sources, 5% for 125I-on-Ag sources, and 5% for 103Pd sources. However, a convincing explanation for this temporary shift has not been determined.

Exhaustive intercomparisons with 1998 brachytherapy calibrations, Loftus transfer chamber readings, and low-energy x-ray beams confirmed that post-January 2000 WAFAC 2K measurements agreed with those performed in 1998. A new comparison of the WAFAC (original) with the Ritz chamber on the NIST x-ray calibration range yielded agreement to ~0.8%. The original and newer automated-WAFACs continued to agree with each other. NIST completed a number of measurements of a 6702 and a 6711 source, comparing the results in the WAFAC (NIST 1999...
standard) and in the re-entrant chamber (NIST 1985 standard). The results indicate a combined ratio for the sources of 0.897±0.028, in very good agreement with the determination made in 1997–1998. This then confirmed the correctness of the WAFAC measurements in 2000–2001 and in 1997–1998, and indicated that the problem was confined to measurements made in 1999 (perhaps including late 1998).

The conclusion is that NIST WAFAC measurements up to mid-1998 and after January 1 2000 are correct, and that current dose-rate constants for the 6702 and 6711 sources, based on the ratio NIST1999/NIST1985=0.897, are valid. However, WAFAC air-kerma strengths measured in 1999 were too large by 2% to 7%, and required dose-rate constant measurements normalized to NIST 1999 $S_K$ calibrations to be revised accordingly. All measured dose-rate constant data given in this protocol have been normalized to the $S_{Kn,1999}$ standard as corrected in January 2000.

APPENDIX C: EVALUATION OF DOSE RATE AT SMALL AND LARGE DISTANCES

Care must be taken in evaluating dose rates at distances falling outside the range of tabulated data, $r_{min}$ and $r_{max}$, especially at $r<0.5$ cm. While difficult to measure, modern Monte Carlo techniques can easily calculate dose rates at distances as small as 0.1 cm from the center of the source. This protocol recommends that $g_X(r)$ data be extracted and tabulated from Monte Carlo-derived dose rates for $r>0.1$ cm if possible. $F_X(r,\theta)$ data are generally not available, even from most Monte Carlo evaluations, at $r<0.25$ cm. At shorter radii, points at small polar angles near $0^\circ$ and $180^\circ$ are located inside the source capsule, implying that $F_X(r,\theta)$ cannot be readily defined over the full angular interval [0°,90°].

Essentially, the TG-43 formalism using a polar coordinate system breaks down at $r<L/2$. Users are warned that when working at small distances it is essential to use the same geometry function and $L$ for evaluating absorbed dose as when used in the conversion of measured or Monte Carlo data in the TG-43 parameter ratios. Often, $F_X(r,\theta)$ and $g_X(r)$ will exhibit nonphysical properties due to breakdown of the line-source $G_L(r,\theta)$ very near the source.

Three separate scenarios are described in the following sections.

1. 2D dose calculations

Evaluation of the 2D dose calculation formalism for distances $r< r_{min}$ or $r>r_{max}$, should be made using the nearest neighbor, zeroth-order approximation for selection of both $F_X(r,\theta)$ and $g_X(r)$,

$$F_X(r,\theta) = \begin{cases} \text{interpolated value,} & r_{min} \leq r \leq r_{max}, \\ F_X(r_{\min},\theta), & r < r_{\min}, \\ F_X(r_{\max},\theta), & r > r_{\max}. \end{cases}$$

(C1)

$g_X(r)$ will follow the same extrapolation approach as recommended for Eqs. (6) and (C1), and approach zero at large distances. Where measured and calculated Monte Carlo data are not available, such as for RTP systems that require $F_X(r,\theta)$ and $g_X(r)$ values at $r=0$, extrapolation using the aforementioned approach is recommended. While a first-order approach using linear extrapolation is also possible, the merits of this approach have not been demonstrated.

Calculation of $G_X(r,\theta)$ should employ Eq. (4) down to distances on the order of the interval between adjacent calculation points. Daskalov et al. have found that the nearest neighbor method introduces uncertainties <2% for 0.1 cm along and away distances. 124

2. Collaborative Ocular Melanoma Study dosimetry

In some specialized applications such as episceral eye plaque therapy, anisotropy corrections are prohibited when following a protocol such as that published by the Collaborative Ocular Melanoma Study (COMS). 11,51,155–158 In eye plaque therapy, the sources are placed in a nearly spherical cup and within the target volume most of the seeds contribute dose along their transverse directions. In this setup, the target volume receives very little dose in the longitudinal directions of the sources. For practical reasons, the COMS protocol has recommended that for dose calculation within the target volume of eye plaque brachotherapy, the seeds can be identified as point sources provided one uses the dose rates on the transverse-plane alone. This procedure results in the following expression for dose rate at different distances from the sources. For distances smaller than $r_{min}$, the nearest neighbor approach should be used with the relevant $r_{min}$ value used in the radial dose function,

$$D(r) = S_K \cdot \frac{g_X(r,\theta)}{G_X(r_{\min},\theta)} \cdot g_X(r_{\min}) \quad \text{for} \quad r<r_{min}. \quad \text{(C2)}$$

3. 1D dose calculations

When anisotropy corrections are needed, and optimal accuracy is desired at distances less than $r_{min}$, the minimum distance for which $\phi_{an}(r)$ is tabulated, the following model can be used to extrapolate dose to short distances:

$$D(r) = \begin{cases} S_K \cdot \frac{G_X(r,\theta)}{G_X(r_{\min},\theta)} \cdot g_X(r_{\min}) \cdot \phi_{an}(r_{\min}), & r<r_{\min}, \\ S_K \cdot \frac{r_{\min}^2}{r} \cdot \frac{g_L(r)}{g_L(r_{\min})} \cdot \frac{G_X(r_{\min},\theta)}{G_X(r_{\min},\theta)} \cdot g_X(r_{\min}) \cdot \phi_{an}(r_{\min}), & r\geq r_{min}. \end{cases} \quad \text{(C3)}$$

For distances $r \geq r_{min}$, $X=P$ and Eq. (C3) is equivalent to the standard 1 formula, Eq. (10). The short-distance extrapolation model ($r<r_{min}$) is based on applying Williamson’s approximation, $r^{-2} \cdot \phi_{an}(r) = G(r,\theta) \cdot \phi_{an}(r)$, to the short distance region, i.e., $r^{-2} \cdot \phi_{an}(r_{\min}) = G(r,\theta) \cdot \phi_{an}(r)$ for $r<r_{min}$. 44
\[ D(r) = S_K \cdot \Lambda \cdot \left( \frac{r_0}{r} \right)^2 \cdot \frac{g_L(r)}{g_L(r_{\text{min}})} \cdot \phi_{\text{an}}(r_{\text{min}}), \]

\[ r < r_{\text{min}}. \]  

(C4)

No matter how sophisticated an extrapolation model is chosen, users should realize that at \( r < 0.25 \) cm where \( \phi_{\text{an}}(r) \) data may not be available due to lack of assessment or due to positioning within the capsule, none of the 1D models described above yield quantitatively meaningful estimates of the solid angle-weighted average dose.

**APPENDIX D: ANISOTROPY CONSTANT**

The definition of the anisotropy constant, \( \bar{\phi}_{an} \), largely remains the same as that presented in TG-43, and is expanded upon. Use of \( \bar{\phi}_{an} \), as commonly practiced at this time, does not exactly reproduce either the measured or Monte Carlo dosimetry data for \( r < 1 \) cm. Therefore, it is strongly recommended that users utilize \( \phi_{an}(r) \) and Eq. (11), or compensate for treatment planning inadequacies using the method outlined in Eq. (14), for implementing 1D dosimetry formalism.

For those users who insist on using \( \bar{\phi}_{an} \), the following implementation will minimize dose-calculation errors at small distances, e.g., \( r \leq 1 \) cm:

\[ D(r) = S_K \cdot \Lambda \cdot \left( \frac{r_0}{r} \right)^2 \cdot g_L(r) \cdot \bar{\phi}_{an}. \]  

(D1)

For this purpose, the inverse-square law weighted average of \( \phi_{an}(r) \) for \( r > 1 \) cm should be used,

\[ \bar{\phi}_{an} = \frac{\sum_{r>1\text{cm}}^{r_{\text{max}}} \phi_{an}(r) \cdot r^{-2}}{\sum_{r>1\text{cm}}^{r_{\text{max}}} r^{-2}}. \]  

(D2)

For instances where \( \phi_{an}(r) \) data are not available over constant increments of \( r \), linear interpolation of \( \phi_{an}(r) \) may be used for derivation of \( \bar{\phi}_{an} \). The constraint on \( r \) is needed because dose distributions near typical brachytherapy sources generally take the shape of prolate ellipsoids due to the dominating effects of solid angle. This is because \( F(r, \theta) \) excludes dose fall-off already included by the geometry function, and \( \phi_{an}(r) \) (and subsequently \( \bar{\phi}_{an} \)) do not. Therefore, \( \phi_{an}(r) \) rapidly increases as \( r < 2L \), and can assume values much larger than unity. While nonintuitive, the use of \( g_L(r) \) with the point-source geometry function in Eq. (D1) better approximates the average dose at small distances than the superficially more consistent expression \( g_X(r) \cdot G_X(r, \theta_0) \cdot \bar{\phi}_{an} \cdot G_X(r_0, \theta_0)^{-1} \) again due to the ellipsoidal shape of the isodose surfaces. Thus \( r^{-2} \cdot \bar{\phi}_{an} \approx g(r, \theta_0) \cdot \phi_{an}(r) \). For sources with \( L \approx 0.3 \) cm, this approximation is sufficiently good that errors introduced are often less than 5% at distances \(< 0.3 \) cm. However, Williamson demonstrated that Eq. (D1) can produce much larger errors for low-energy sources with longer effective active lengths. Because of this short-distance behavior, the following forms should not be used at \( r < 0.5 \) cm:

\[ D(r) = S_K \cdot \Lambda \cdot \left( \frac{r_0}{r} \right)^2 \cdot g_P(r) \cdot \bar{\phi}_{an}. \]

or

\[ D(r) = S_K \cdot \Lambda \cdot \frac{G_L(r, \theta_0)}{G_L(r_0, \theta_0)} \cdot g_L(r) \cdot \bar{\phi}_{an}. \]  

(D3)

**APPENDIX E: APPARENT ACTIVITY**

The quantity apparent activity, \( A_{\text{app}} \), is defined as the activity of an unfiltered point source of a given radionuclide that has the same air-kerma strength as that of the given encapsulated source. It has been widely used by vendors and customers alike to specify the strength of sealed radioactive sources such as \(^{125}\)I, \(^{103}\)Pd and \(^{198}\)Au. Furthermore, \( A_{\text{app}} \) is used in the treatment planning of permanent implants using \(^{103}\)Pd and \(^{252}\)Cf interstitial sources. Using the apparent activity as a method of source strength specification suffers from a number of problems. For example, vendors using apparent activity to report source strength in essence convert a statement of source output, e.g., \( S_K \), into \( A_{\text{app}} \) by dividing \( S_K \) by an assumed value of the exposure rate constant (\( \Gamma_X \)). To calculate absorbed dose in a medium around such sources, users shall multiply the vendor supplied \( A_{\text{app}} \) value by the same (\( \Gamma_X \)) value. Although (\( \Gamma_X \)) is a clearly defined physical concept, it has no meaningful physical role in the dosimetry of output calibrated sources. Continued use of such dummy constants constitutes a significant potential source of dosimetric error since the user may choose the wrong (\( \Gamma_X \)) value. It is essential that users employ the same (\( \Gamma_X \)) values as the manufacturer for dosimetric calculations rather than more physically accurate or definitive values taken from the recent literature.

In 1999, NIST implemented a new primary standard for air-kerma strength. The AAPM has consistently taken the position that \( S_K \) should be the quantity used for specifying brachytherapy source strength for the purpose of defining calibration standards, documenting source strength on calibration reports and for all aspects of dose calculation and treatment prescription. Both users and vendors shall take appropriate steps to adopt this new source-strength standard correctly. To facilitate an unambiguous conversion of source strength estimates and for transitional practice, the LIBD has recommended a set of data and equations for the conversion of (\( S_K/A_{\text{app}} \)) for \(^{125}\)I and \(^{103}\)Pd interstitial brachytherapy sources. For all \(^{125}\)I and \(^{103}\)Pd sources, regardless of internal construction, the values of (\( \Gamma_X \)) recommended were 1.45 and 1.476 \( \text{R cm}^2 \text{mCi}^{-1} \text{h}^{-1} \), respectively. When implementing the TG-43 formalism based upon apparent activity specification, the recommended (\( S_K/A_{\text{app}} \)) conversion coefficients were 1.27 and 1.293 \( \mu\text{Gy cm}^2 \text{h}^{-1} \text{mCi}^{-1} \) for \(^{125}\)I and \(^{103}\)Pd, respectively. The authors discussed the importance of using a consistent set of values for the exposure rate constant (\( \Gamma_X \)) for the evaluation of (\( S_K/A_{\text{app}} \)). For example, adopting \( S_K \)-to-\( A_{\text{app}} \) conversion coefficients derived from modern (\( \Gamma_X \)) values, different from the ones used by the authors; would require all users and vendors to redefine the relationship between \( S_K \) and \( A_{\text{app}} \); would require updating of dosi-
metric constants in all $A_{\text{app}}$-based treatment planning systems; could cause significant confusion among clinical users; would complicate future retrospective analyses of clinical outcome data; and would not improve dosimetric accuracy. This further emphasizes the importance of using the same value of $(\Gamma_g)_{\text{app}}$ by the vendors and the users. Consequently, the AAPM continues to recommend that the quantity $A_{\text{app}}$ not be used for specification of brachytherapy source strength.


D. S. Waid, M. J. Rivard, and J. G. Wierzbicki, “The 0.897 factor is not used to convert S E,155 to S E,990 when performing Monte Carlo calculations to calculate the dose rate constant,” Med. Phys. (accepted).


G. S. Ibbott, A. S. Meigooni, and D. M. Gearheart, “Monte Carlo deter-


